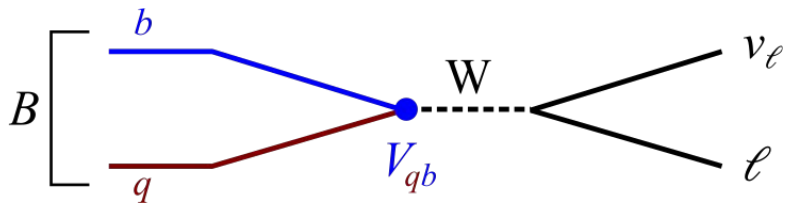
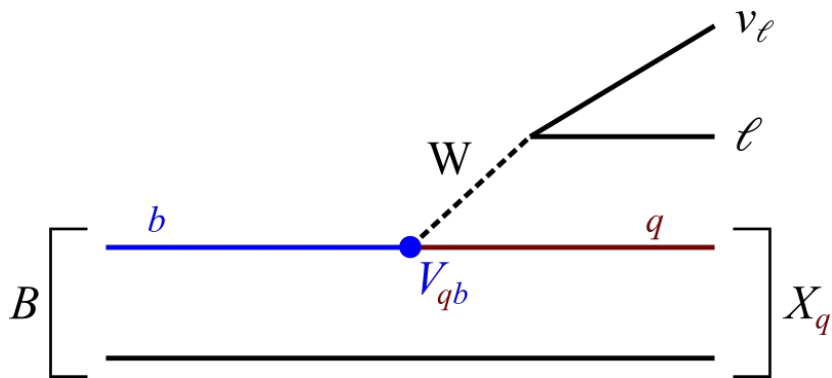
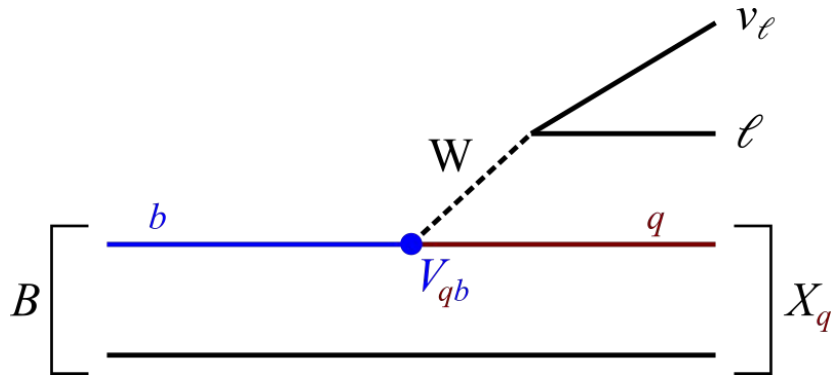


# Semileptonic and Leptonic $B$ decays

PIC 2019 TAIPEI

PETER M. LEWIS | BONN

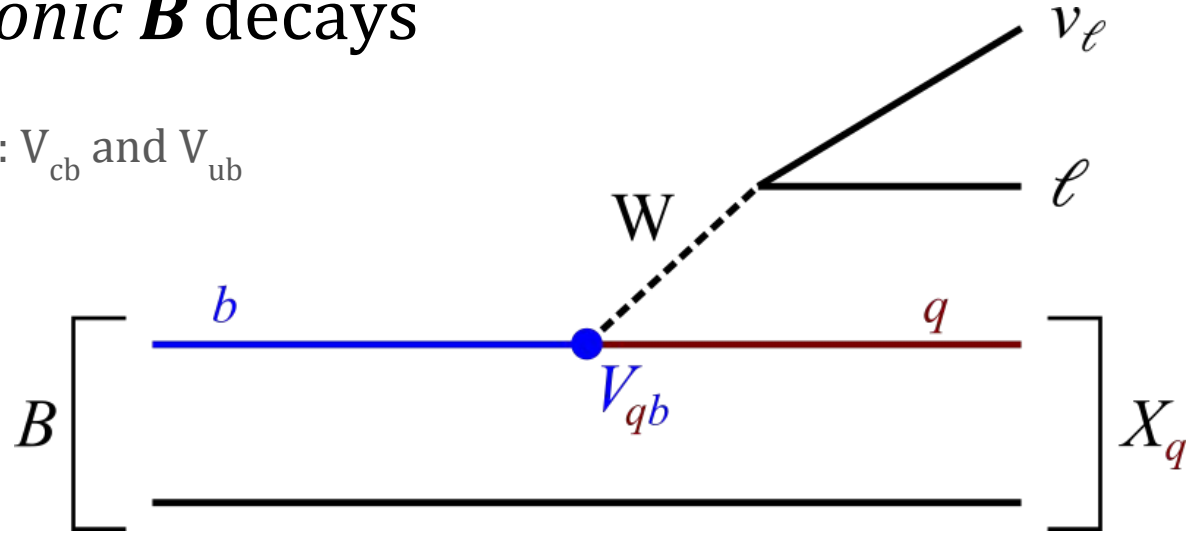




## SEMILEPTONIC B DECAYS

# Semileptonic $B$ decays

A **CKM** probe:  $V_{cb}$  and  $V_{ub}$

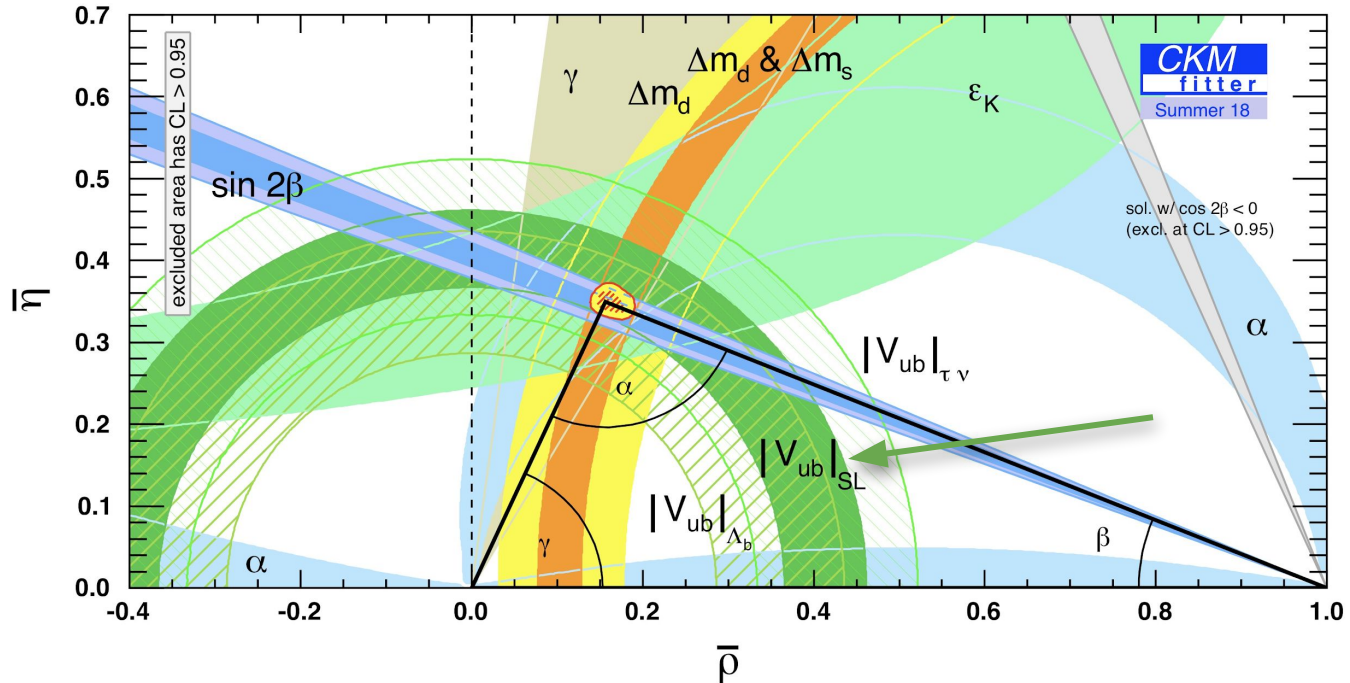


	d	s	b
u	■	■	·
c	■	■	■
t	·	■	■

Two red arrows point to the  $b$  column of the CKM matrix, highlighting the elements  $V_{ub}$  and  $V_{cb}$ .

# Semileptonic $B$ decays

A **CKM** probe:  $V_{cb}$  and  $V_{ub}$



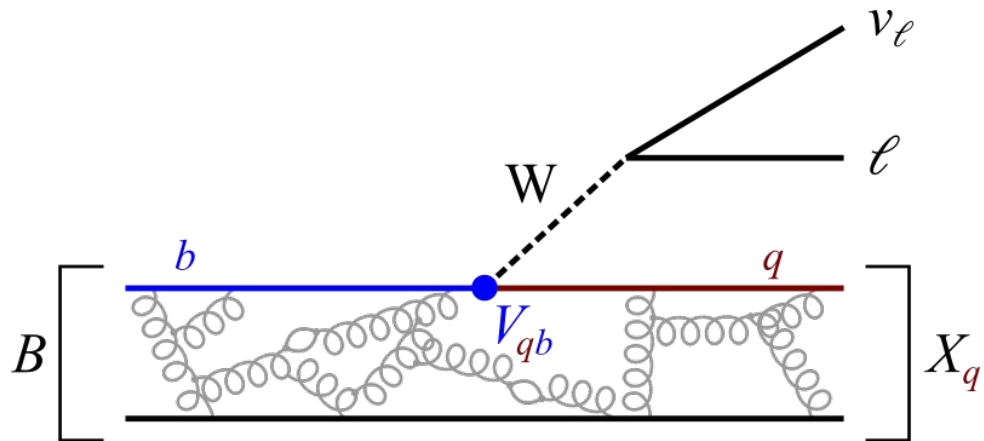
# Semileptonic $B$ decays

Theory: exclusive decays

- Tree-level diagram has **non-perturbative QCD muck**
- Parameterize in terms of the momentum transfer squared  $q^2 = (p_\ell + p_\nu)^2$ :

$$\frac{d\Gamma}{dq^2} \propto |V_{xb}|^2 |f(q^2)|^2$$

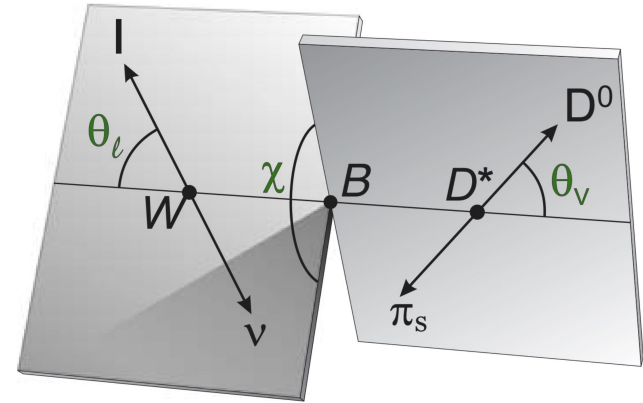
- Form factors tied to light cone sum rules (low  $q^2$ ) or lattice calculations (high  $q^2$ )
- (three additional angular parameters needed in decays to vector mesons like  $\rho$ ,  $D^*$ )



# Semileptonic $B$ decays

Theory: form factor parameterization

- (as an example: exclusive  $B \rightarrow D^* l \nu$ )
- Form factor  $F$ : terms for **three helicity amplitudes**
- **CLN**: (Caprini, Lellouch, Neubert)
  - **HQET** input to reduce number of free parameters to 3; extract from experiment
- **BGL**: (Boyd, Grinstein, Lebed)
  - Expand each FF in the most generic form, with minimal assumptions, in a power series
- **CLN** was standard for 20 years, but **BGL** is gaining favor due to **model-independent approach**
  - **Some implications for validity of HQET**

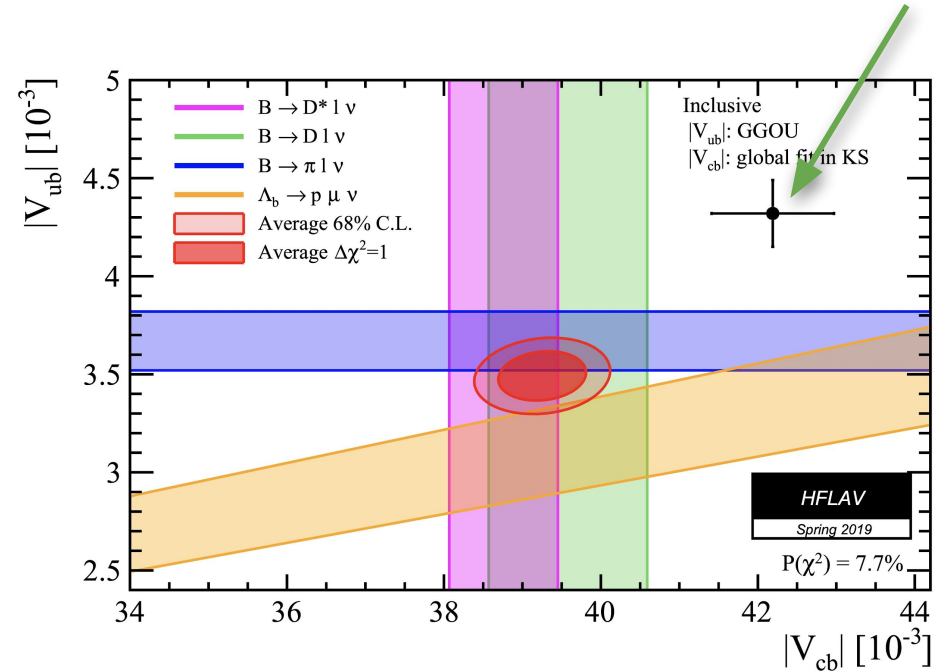


$$\frac{d\Gamma(B \rightarrow D^{*-} \ell^+ \nu)}{dw d\cos\theta_\ell d\cos\theta_\nu d\chi} = \frac{G_F^2 |V_{cb}|^2}{48\pi^3} F(w, \cos\theta_\ell, \cos\theta_\nu, \chi) G(w)$$

# Semileptonic $B$ decays

## An interesting puzzle

- Tension in  $V_{cb}$  and  $V_{ub}$  between *inclusive* vs. *exclusive* reconstructions
- (exclusive results here use **CLN**)



# Semileptonic $B$ decays

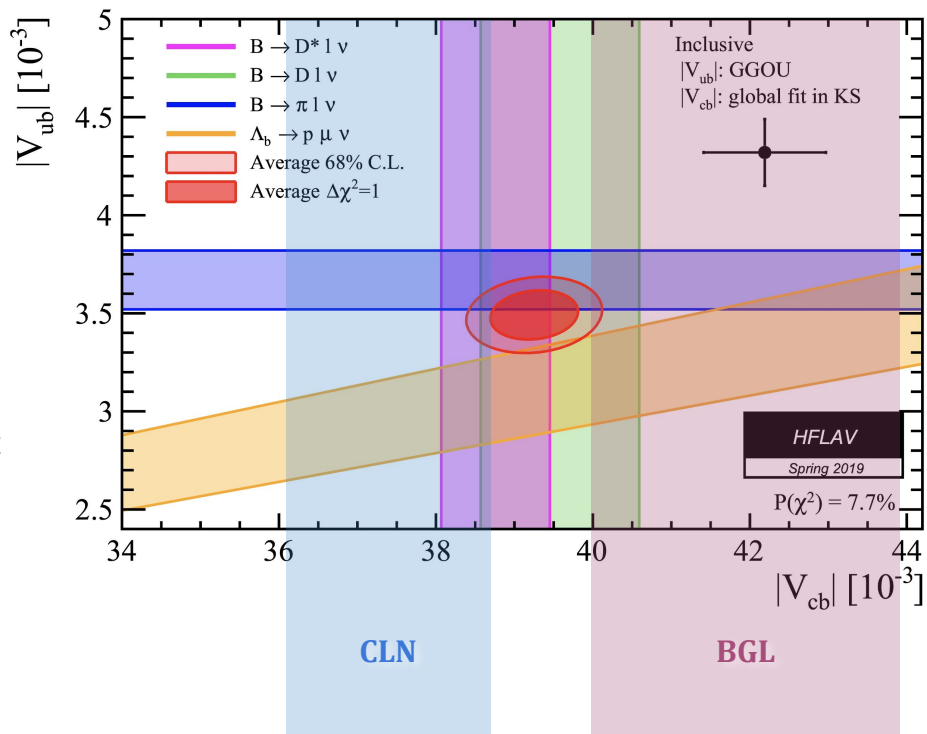
## An interesting puzzle: *a solution?*

- Two 2017 re-parameterizations of Belle's extraction of  $|V_{cb}|$  in  $B \rightarrow D^* l \nu$ :
  - **CLN** consistent with HFLAV exclusive average
  - **BGL** more consistent with inclusive
- Is exclusive/inclusive tension entirely a result of form factor parameterization?
- New developments to be discussed!

While our findings do not provide a clear resolution of the  $|V_{cb}|$  puzzle, they strongly question the reliability of the current  $B \rightarrow D^* l \nu$  averages [3] and call for a reanalysis of old experimental data before Belle-II comes into action.

Belle tagged  $B \rightarrow D^* l \nu$ , 2017  
[arxiv:1702.01521](https://arxiv.org/abs/1702.01521)

Reparameterizations, 2017  
[arxiv:1703.06124](https://arxiv.org/abs/1703.06124)  
[arxiv:1703.08170](https://arxiv.org/abs/1703.08170)





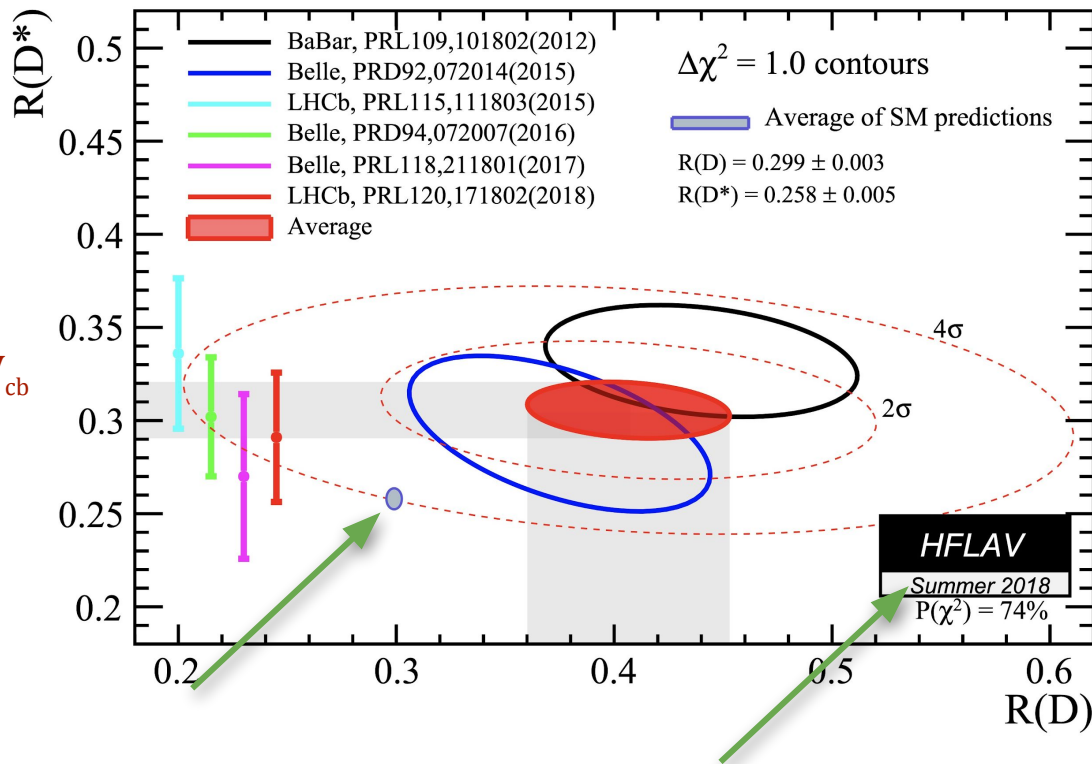
# Semileptonic $B$ decays

## Another interesting puzzle

- Signs of lepton universality violation?

$$R(D^{(*)}) = \frac{\mathcal{B}(B \rightarrow D^{(*)}\tau\nu)}{\mathcal{B}(B \rightarrow D^{(*)}l\nu)}$$

- (ratio removes dependence on  $V_{cb}$  and cancels some theoretical+experimental uncertainties)



# Semileptonic $B$ decays

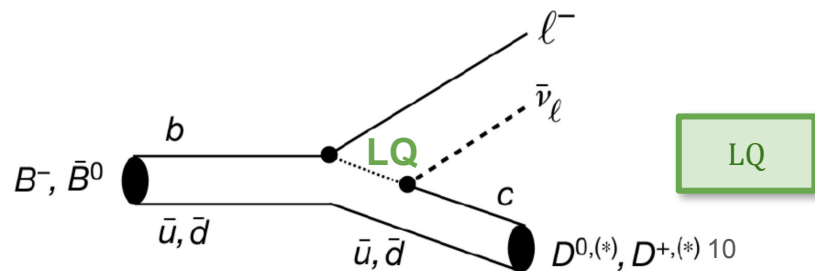
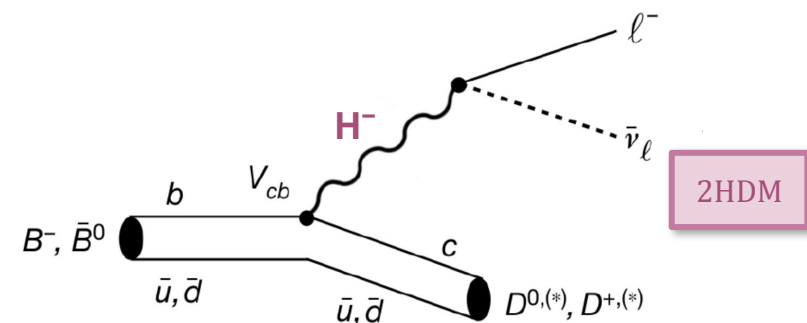
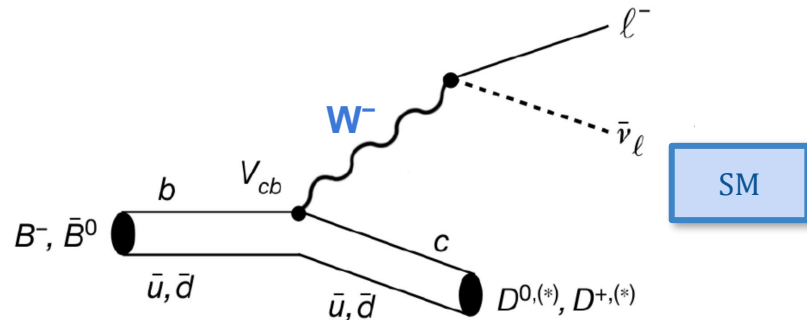
Another interesting puzzle:  $R(D^{(*)})$

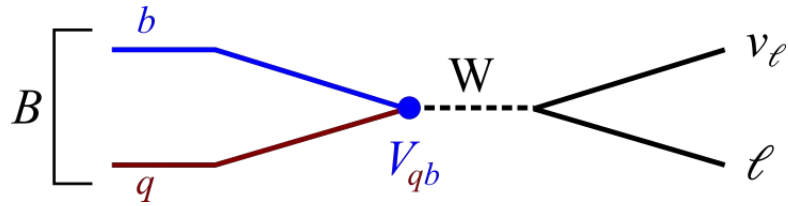
- $R(D^{(*)})$  Sensitive to NP (for example, **charged Higgs**):

$$\mathcal{H}_{\text{eff}} = \frac{G_F}{\sqrt{2}} V_{cb} \left\{ [\bar{c}\gamma^\mu(1-\gamma_5)b][\bar{\ell}\gamma_\mu(1-\gamma_5)\nu_\ell] \right.$$

$$\left. - \frac{m_b m_\tau}{m_B^2} \bar{c}[g_S + g_P\gamma_5]b[\bar{\ell}(1-\gamma_5)\nu_\ell] \right\} + h.c.$$

- Could be sensitive to **leptoquark** models too (additional tensor operator)
- New developments to be discussed!

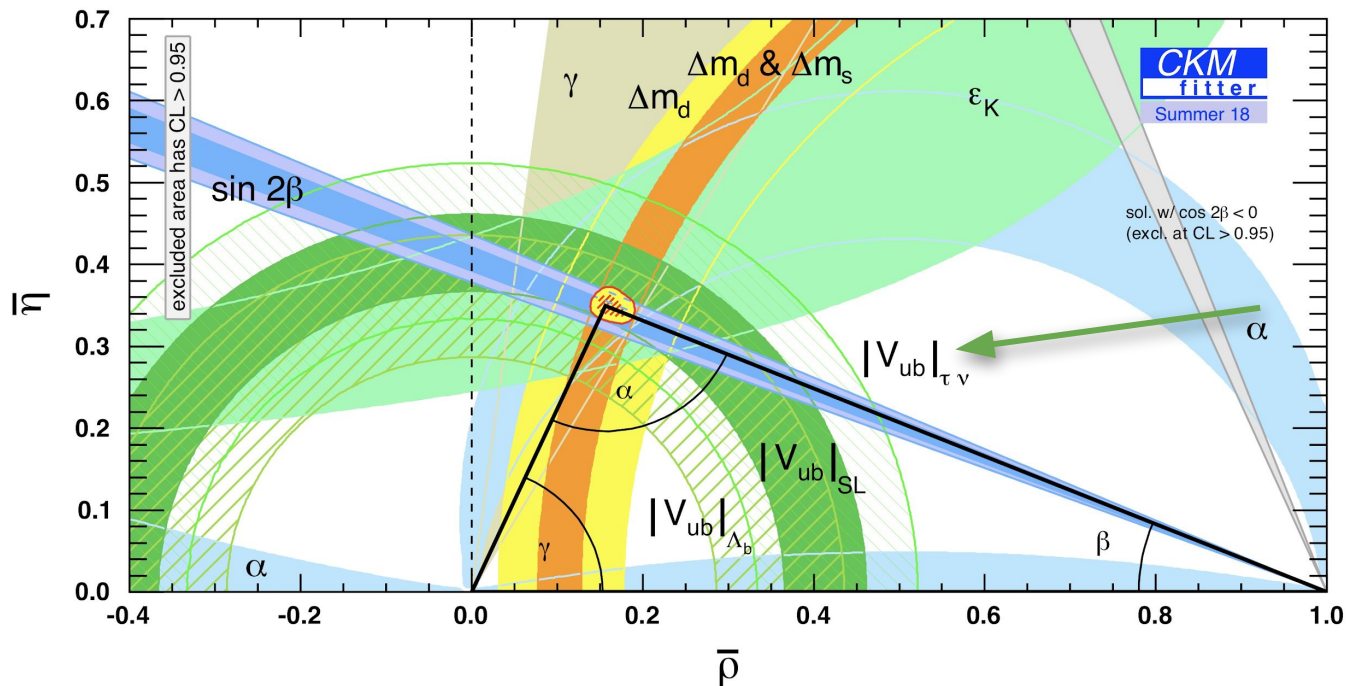




## LEPTONIC $B$ DECAYS

# Leptonic $B$ decays

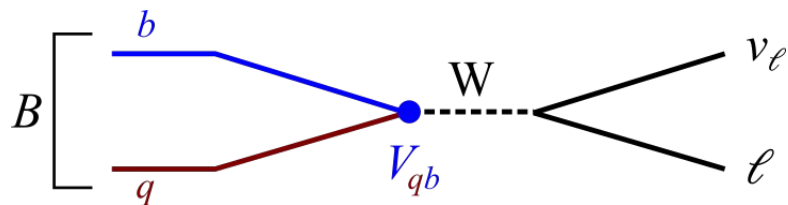
A CKM probe:  $V_{ub}$



# Leptonic $B$ decays

## Theory (exclusive)

- Decay rate (leading-order):
  - Theoretically very clean; precise SM prediction
  - $\Gamma(B \rightarrow \ell\nu) \propto f_B^2 |V_{ub}|^2 x^2 (1-x)^2$
  - **Decay constant  $f_B$**  from QCD sum rules or lattice calculations
  - Helicity suppression factor ( $x = m_\ell/m_B$ ) favors tau mode



# Leptonic $B$ decays

Theory: NP potential

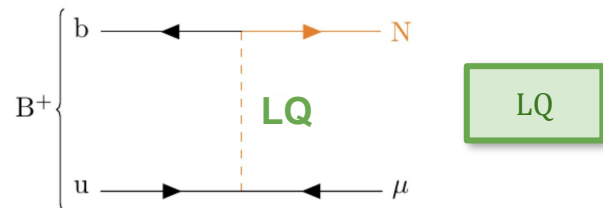
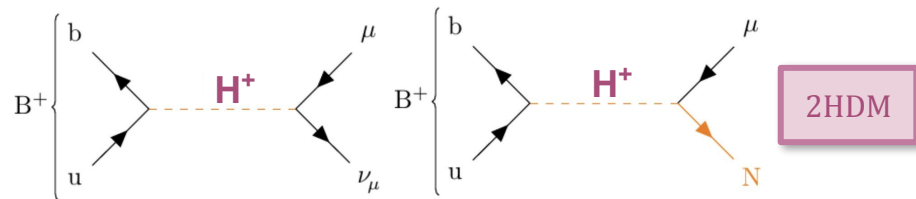
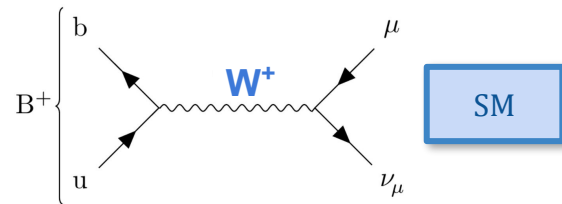
- Sensitive to NP (for example, **charged Higgs**):

$$\mathcal{H}_{\text{eff}} = \frac{G_F}{\sqrt{2}} V_{ub} \left\{ [\bar{u}\gamma^\mu(1-\gamma_5)b][\bar{l}\gamma_\mu(1-\gamma_5)\nu_l] - \tan^2\beta \frac{m_b m_l}{m_H^2} [\bar{u}(1+\gamma_5)b][\bar{l}(1-\gamma_5)\nu_l] \right\} + h.c.$$

- Lepton flavor-independent BF enhancement:

$$\mathcal{B}(B^- \rightarrow l^- \bar{\nu}) = \mathcal{B}_{\text{SM}} \left[ 1 - \tan^2\beta \frac{m_B^2}{m_H^2} \right]^2$$

- Could be sensitive to **leptoquark** models and/or reveal **sterile neutrinos**
- New developments to be discussed!





MEASUREMENT



**BABAR**

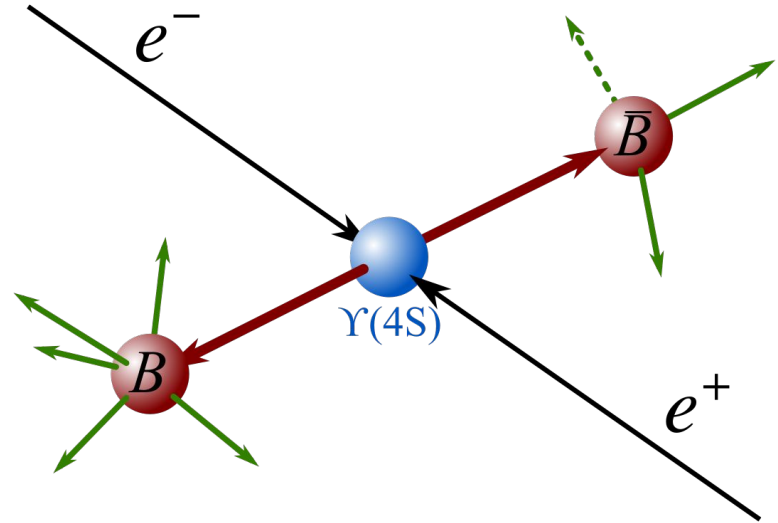


# The $B$ factories

High luminosity, low cross-section, low background, high efficiency

- Experiments
  - Babar (1999-2008): 471 million  $BB$  ( $424 \text{ fb}^{-1}$ )
  - Belle (1999-2010): 771 million  $BB$  ( $711 \text{ fb}^{-1}$ )
  - Belle II (2019-): target **50  $\text{ab}^{-1}$**

See **Shuji Tanaka's** talk tomorrow for Belle II status







**BABAR**

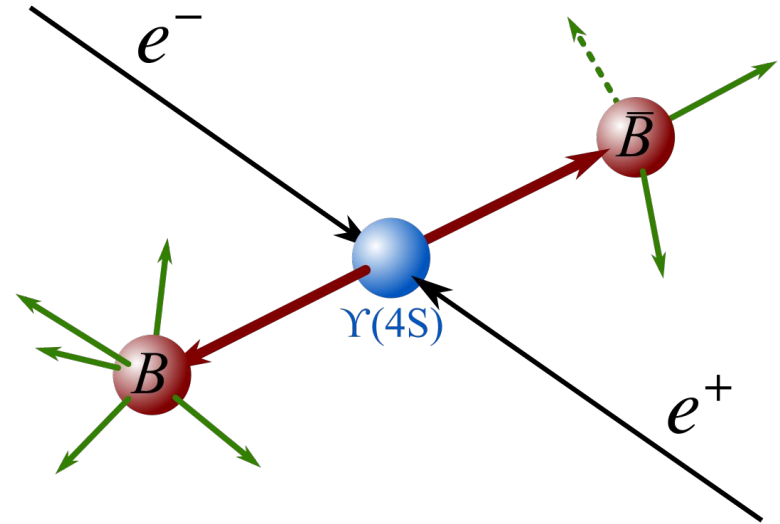
**B**  
BELLE

**B**  
Belle II

# The $B$ factories

High luminosity, low cross-section, low background, high efficiency

- The essentials
  - Electron/positron collision at  $\Upsilon(4S)$  [or higher]  $bb$  resonance (10.58 GeV)
    - Decays  $\sim 100\%$  of time to  $\sim$ at-rest  $BB$  pairs
    - **Kinematics completely known**
  - $\sim 4\pi$  detector coverage
  - Efficient reconstruction of neutrals
  - Very clean environment

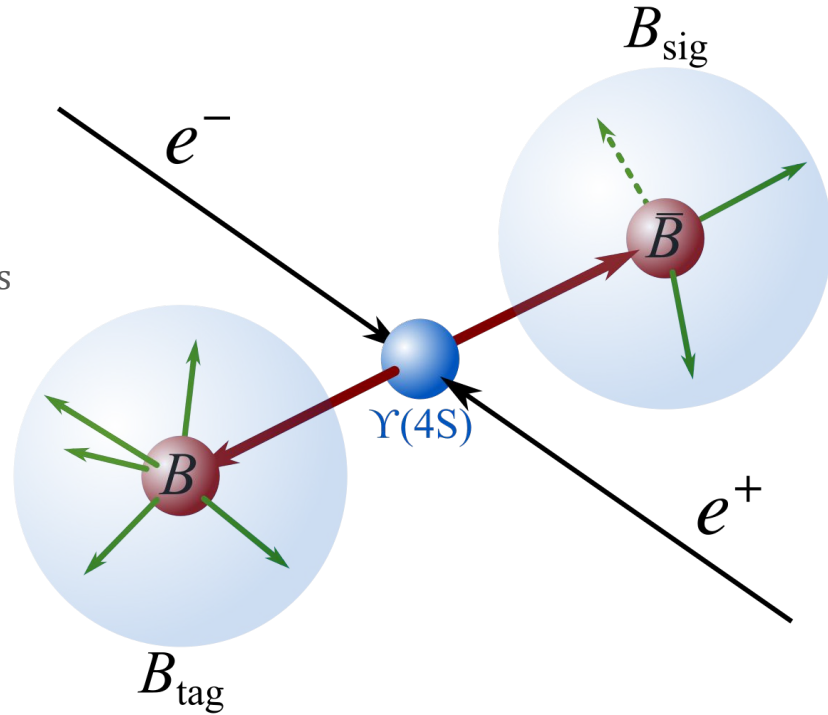




# The $B$ factories

## Tagging

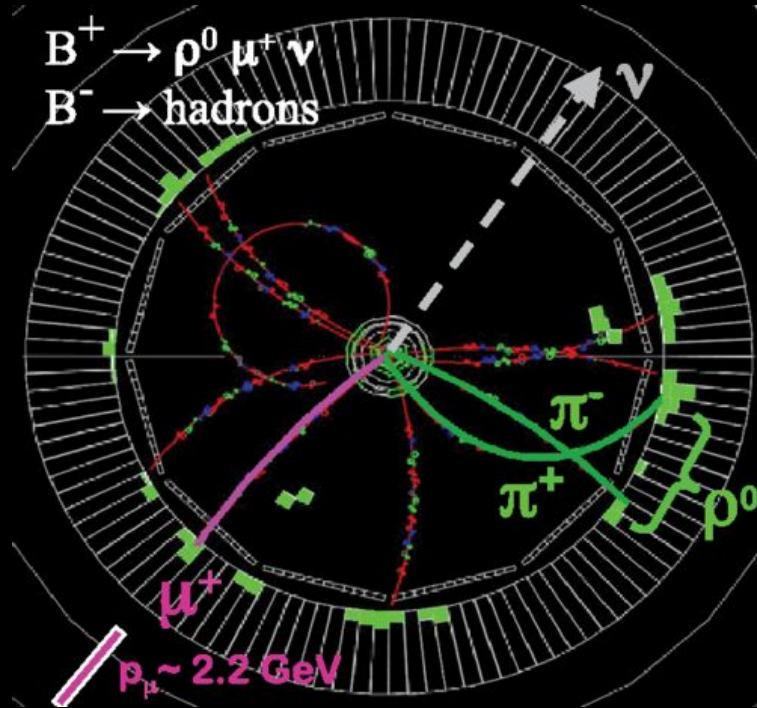
- Full (hadronic) tagging
  - Reconstruct  $B_{\text{tag}}$  in one of  $>10,000$  hadronic modes
  - $p_{\text{tag}}$  now known; thus  $p_{\text{sig}}$  is too
  - $p_v$  now recoverable
  - Tight kinematic constraints now possible; very pure signal selection
  - Downside: tagging efficiency  $\sim 0.1\%$
- Semileptonic tagging
  - Higher tagging efficiency ( $\sim 1\%$ )
  - Weaker kinematic constraints ( $B_{\text{tag}}$  not fully recovered)





**BABAR**

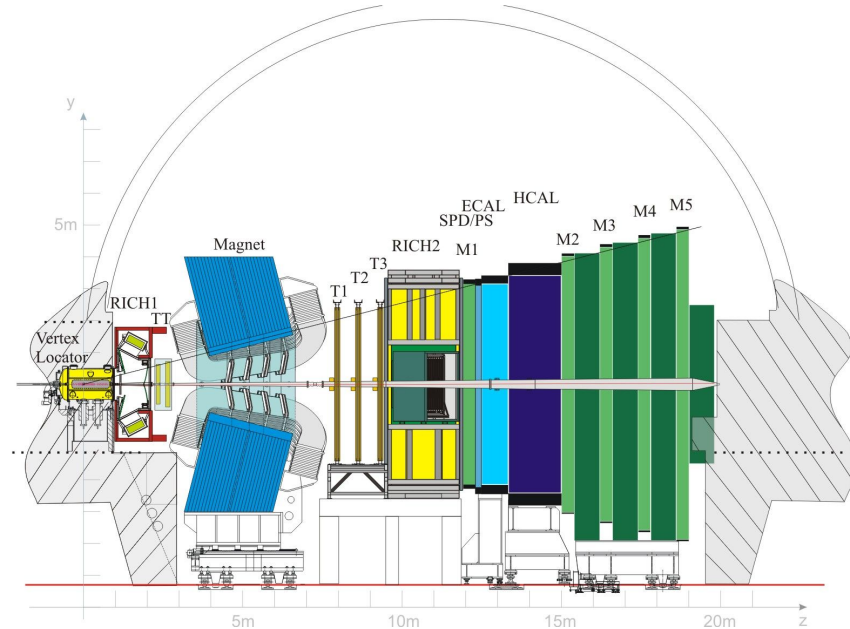
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# LHCb

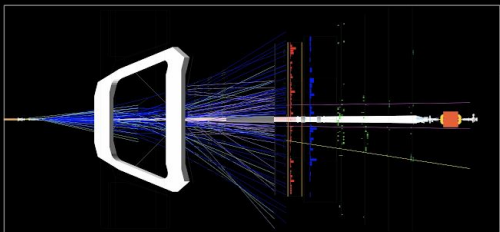
**Low** luminosity, **high** cross-section

- The essentials
  - Proton/anti-proton collision at  $\sim 10\text{TeV}$
  - To date:  $9\text{ fb}^{-1}$
  - Forward coverage only; **large boost**
  - Excellent vertexing ( $\sim\text{cm}$  displacement)
  - Access to *strange* B mesons/baryons
- A generalization:
  - B-factories best for final states with **neutrals** or **missing energy** (e.g.  $B^+ \rightarrow \pi^0 l^+ \nu$ )
  - LHCb best for **charged** final states (e.g.  $B_s^0 \rightarrow \mu\mu$ )
  - **Competitive and complementary**

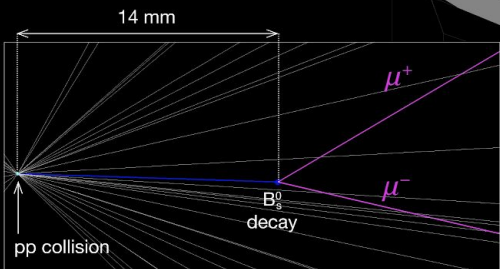
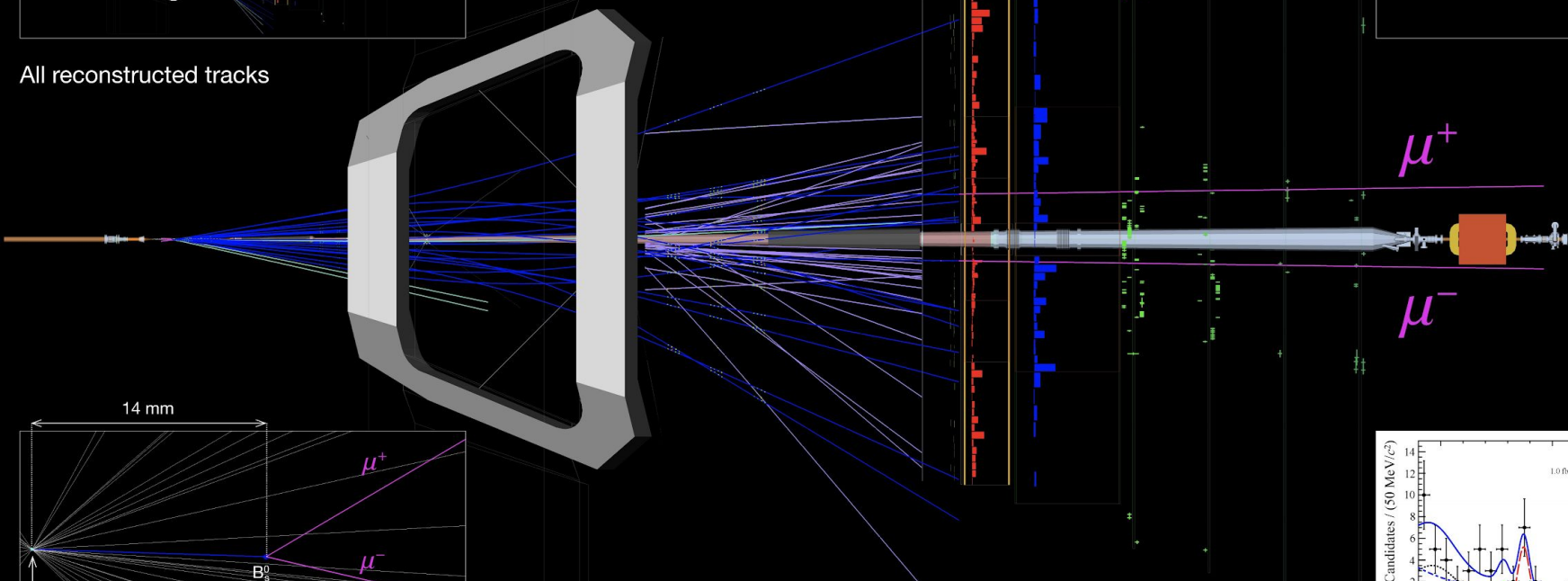
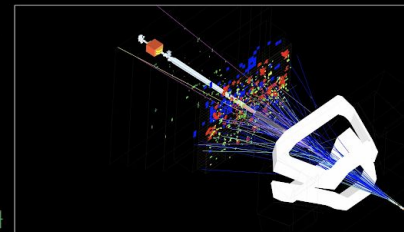


See **Mark Smith's** talk tomorrow for recent LHCb results

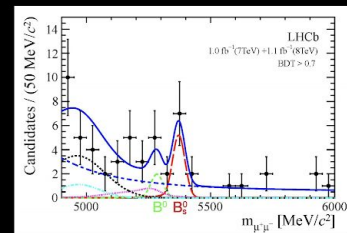
$$B_s^0 \longrightarrow \mu^+ \mu^-$$

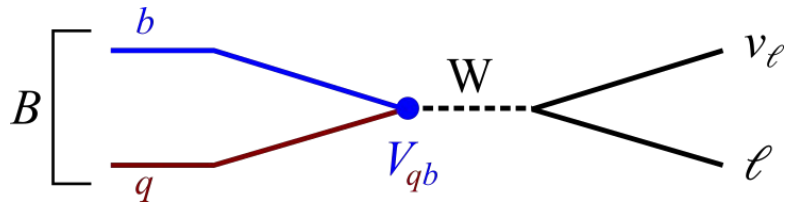
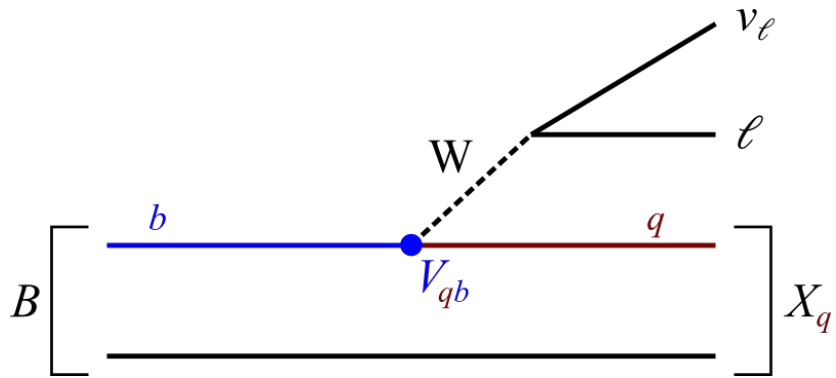


All reconstructed tracks



Only well reconstructed tracks with  $p_T > 500$  MeV





## RECENT DEVELOPMENTS



# Belle: update to $R(D)$ and $R(D^*)$

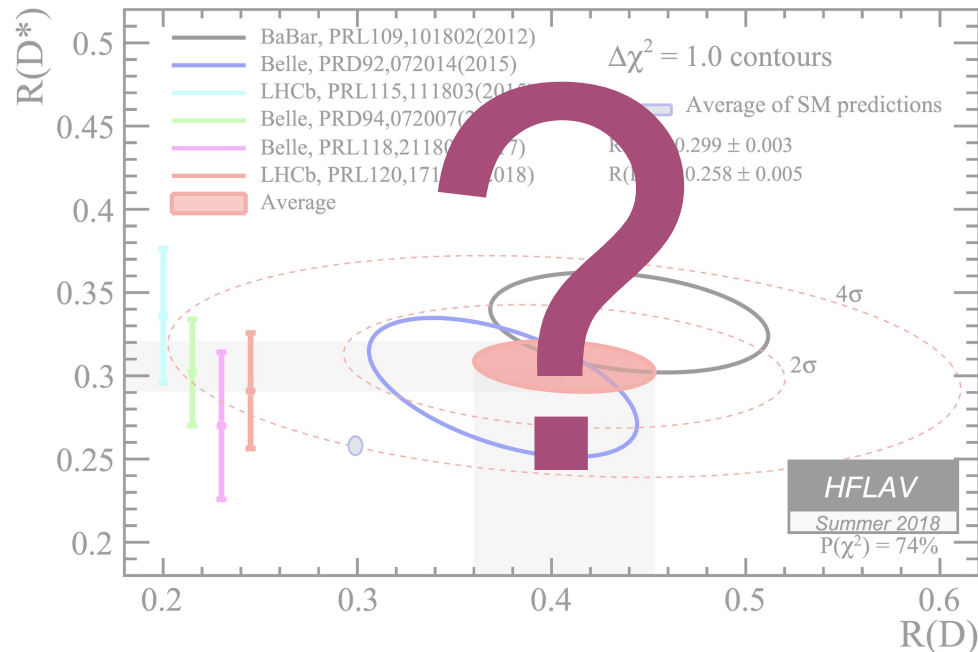
Using *semileptonic* tagging

- (posted to arXiv Apr. 2019)

# Belle: update to $R(D)$ and $R(D^*)$

## Using *semileptonic* tagging

- (posted to arXiv Apr. 2019)
- **First  $R(D)$  measurement using SL tag**
- Improvements vs. older analysis
  - $R(D^*)$  only  $\rightarrow R(D)$  and  $R(D^*)$  simultaneously
  - For  $R(D^*)$ ,  $B^0$  only  $\rightarrow B^\pm, B^0$
  - Improved tagging algorithm (“Full Event Interpretation” from Belle II, [arXiv:1807.08680](https://arxiv.org/abs/1807.08680))

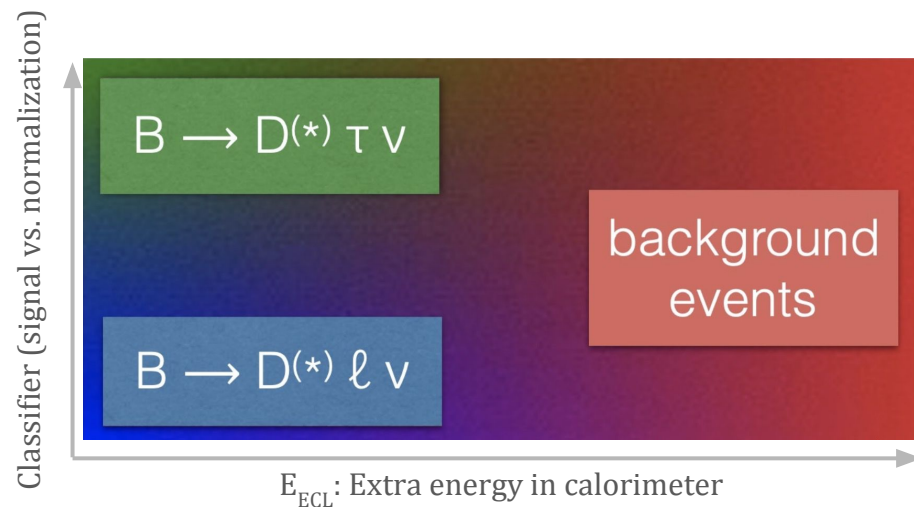




# Belle: update to $R(D)$ and $R(D^*)$

## Using *semileptonic* tagging

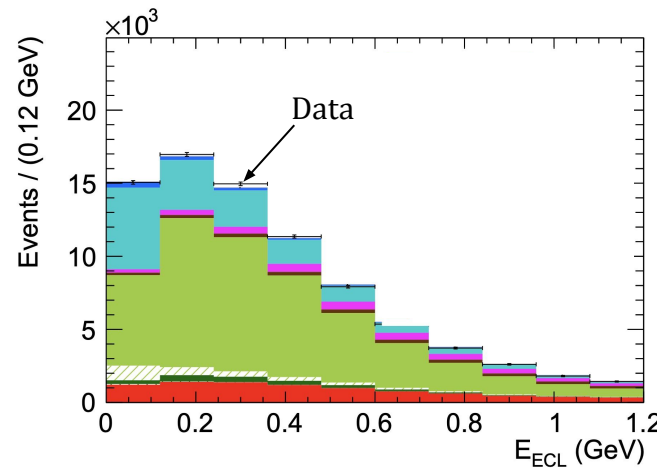
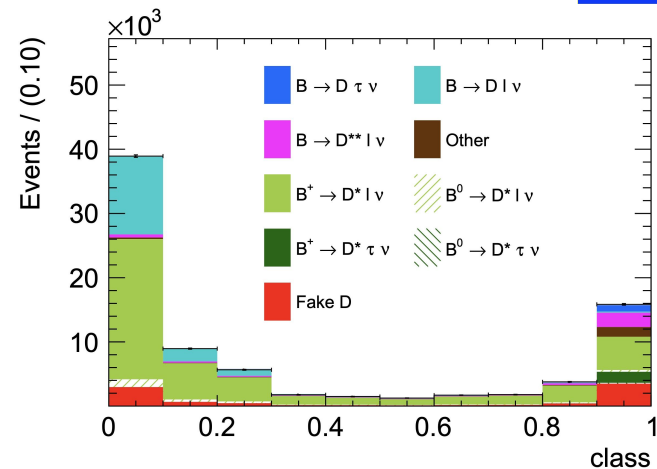
- Simultaneous extraction of all  $B \rightarrow D^{(*)} l \tau \nu$ 
  - Use  $B \rightarrow D^{(*)} l \nu$  as “normalization” mode
- Extraction: 2D fit to:
  - $E_{\text{ECL}}$ : *extra energy* in calorimeter (not associated with tag or signal, right)
  - Signal **classifier** from a BDT trained on *signal against normalization* mode



# Belle: update to $R(D)$ and $R(D^*)$

Using *semileptonic* tagging

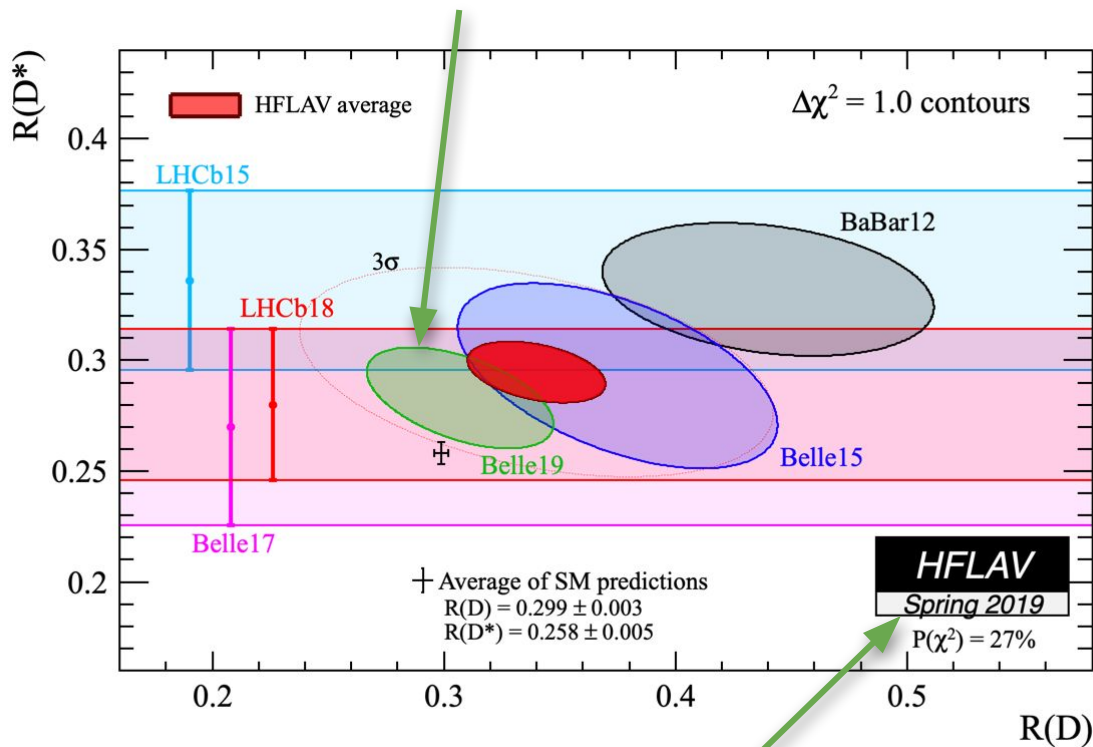
- Fit projections, right, for  $D^0 l$  samples



# Belle: update to $R(D)$ and $R(D^*)$

## Preliminary findings

- Most-precise  $R(D)/R(D^*)$  measurement to date
  - (final word from Belle?)
- Compatible with SM at  $1.2\sigma$ 
  - (possibly decreasing before publication)
- **Belle II results eagerly awaited**





# Belle: $D^*$ polarization in $B^0 \rightarrow D^{*-} \tau^+ \nu_\tau$

A new angle on  $R(D^*)$

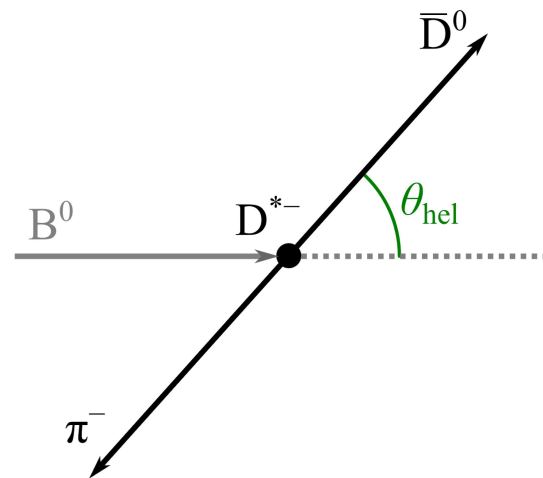
- (preliminary)

# Belle: $D^*$ polarization in $B^0 \rightarrow D^{*-} \tau^+ \nu_\tau$

A new angle on  $R(D^*)$

- (preliminary)
- Probe of **NP** signature in angular distributions
- Target the *fraction of  $D^*$  longitudinal polarization*,  $F_L^{D^*}$

$$\frac{1}{\Gamma} \frac{d\Gamma}{d \cos \theta_{\text{hel}}} = \frac{3}{4} (2F_L^{D^*} \cos^2 \theta_{\text{hel}} + (1 - F_L^{D^*}) \sin^2 \theta_{\text{hel}})$$

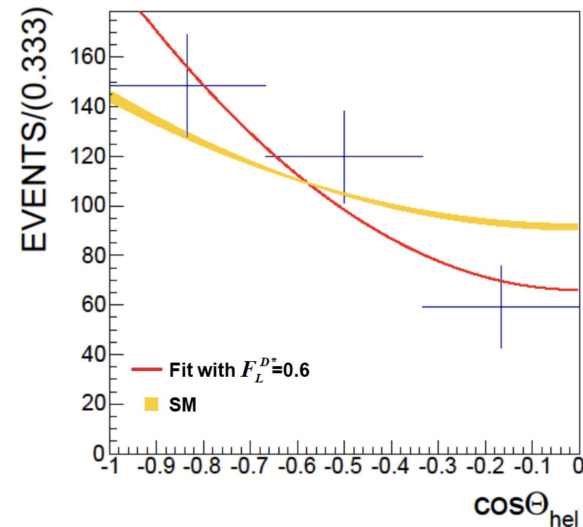


# Belle: $D^*$ polarization in $B^0 \rightarrow D^{*-} \tau^+ \nu_\tau$

## Analysis/results

- *Inclusive* tag
- In each of three  $\cos\theta_{\text{hel}}$  bins, yield comes from fit to **tag** kinematic distributions
- Result agrees with SM within  $1.6\sigma$ :

$$F_L^{D^*} = 0.60 \pm 0.08(\text{stat}) \pm 0.04(\text{syst})$$



BaBar: tagged  $B \rightarrow D^* l \nu$

New analysis probing HQET



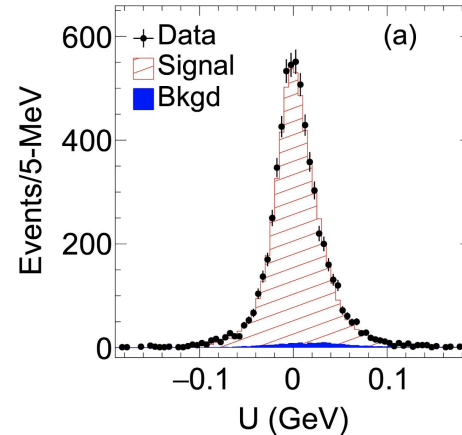
Babar hadronic tagged  $B \rightarrow D^* l \nu$ , 2019

[PRL:123.091801](https://arxiv.org/abs/1203.0918)

# BaBar: tagged $B \rightarrow D^* l \nu$

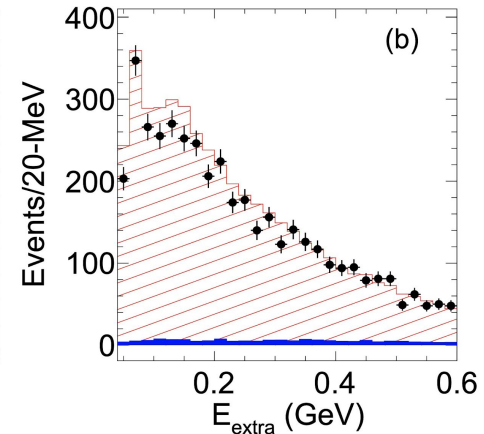
## New analysis probing HQET

- Hadronic-tagged full angular analysis
- Unbinned 4D fit to the 4 kinematic parameters
- A clean probe to HQET assumptions that differentiate **CLN** and **BGL**
- Tight kinematic constraints lead to ultra-pure sample, *right*



$$U = E_{\text{miss}} - |\vec{p}_{\text{miss}}|$$

(inferred neutrino mass)

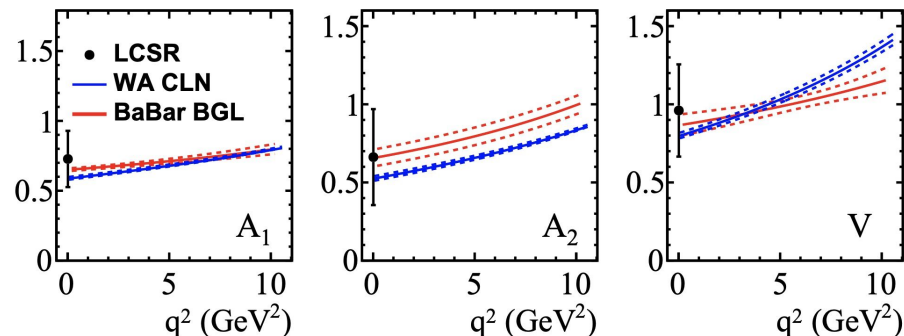




# BaBar: tagged $B \rightarrow D^* l \nu$

## Results

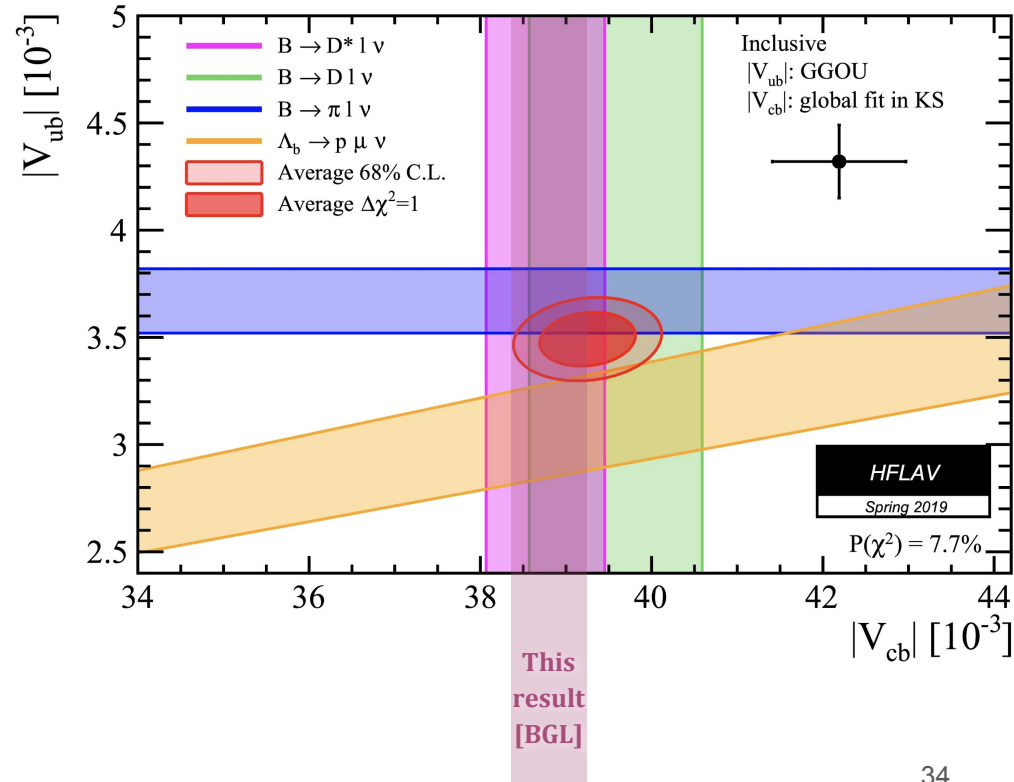
- Form factor shapes with BGL
  - Comparison with world-average CLN
  - Slightly better agreement with zero-recoil ( $q^2=0$ ) LCSR
  - Significant tension in extrapolations to higher  $q^2$
  - **BGL is in tension with HQET**



# BaBar: tagged $B \rightarrow D^* l \nu$

## Results

- Updated  $V_{cb}$  with **BGL**
  - Consistent with CLN world average
  - Parameterization with BGL **does not appear to solve the inclusive/exclusive tension**





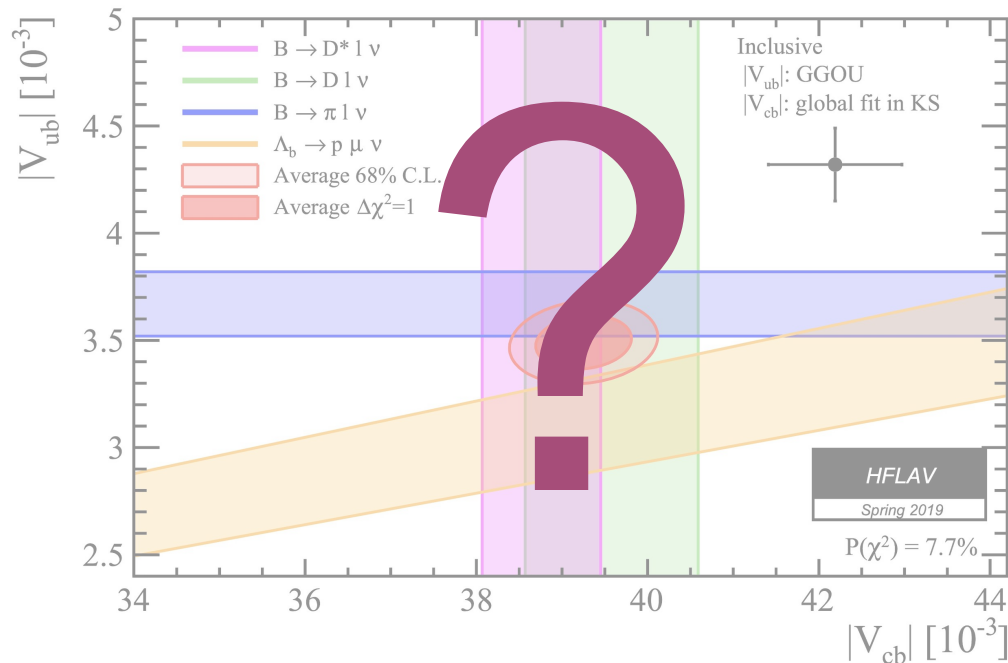
# Belle: untagged $B \rightarrow D^* l \nu$

New analysis comparing CLN and BGL

# Belle: untagged $B \rightarrow D^* l \nu$

New analysis comparing CLN and BGL

- **Highest-precision  $|V_{cb}|$  determination yet**
  - Systematics improvements over prior Belle result
- **First direct measurement using BGL**

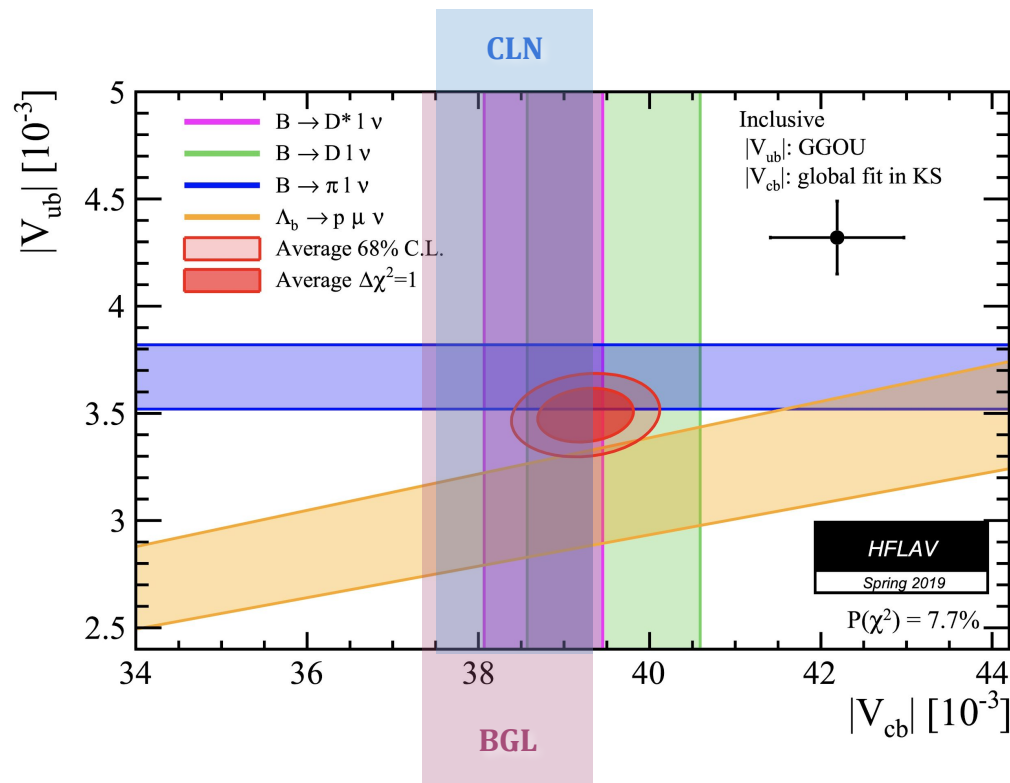


# Belle: untagged $B \rightarrow D^* l \nu$

## Quick summary

- The inclusive/exclusive question is **unresolved**

See **Eiasha Waheed's** talk tomorrow for the details!





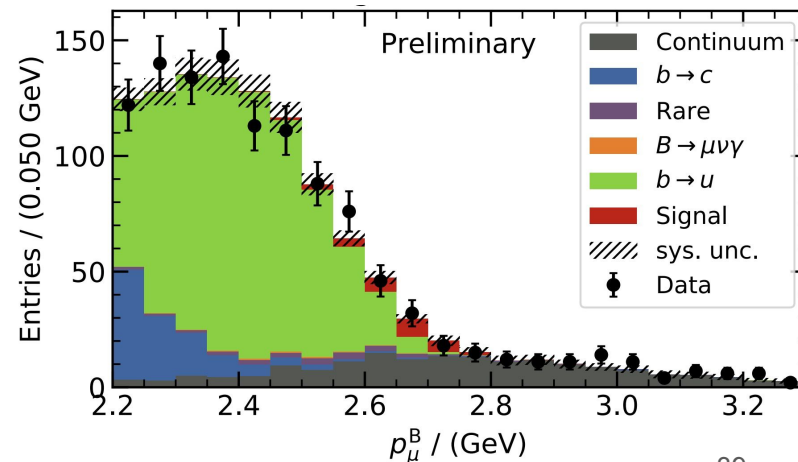
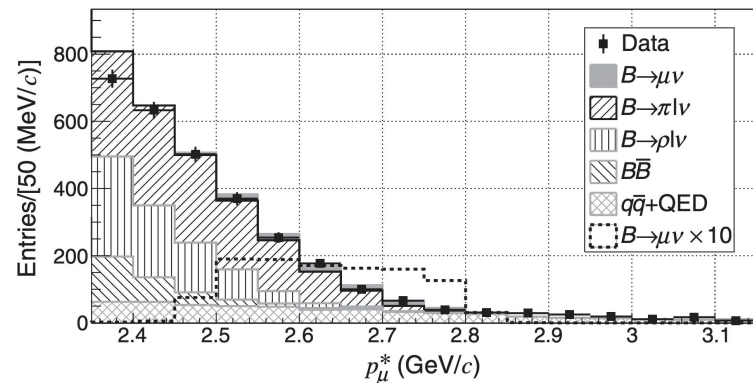
# Belle: update to $B^- \rightarrow \mu^- \nu$

**Preliminary** update to Belle 2018 PRL

# Belle: update to $B^- \rightarrow \mu^- \nu$

## Preliminary update to Belle 2018 PRL

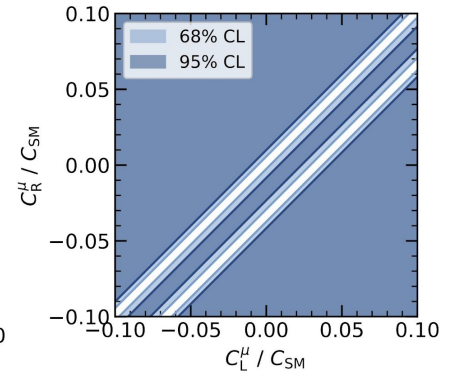
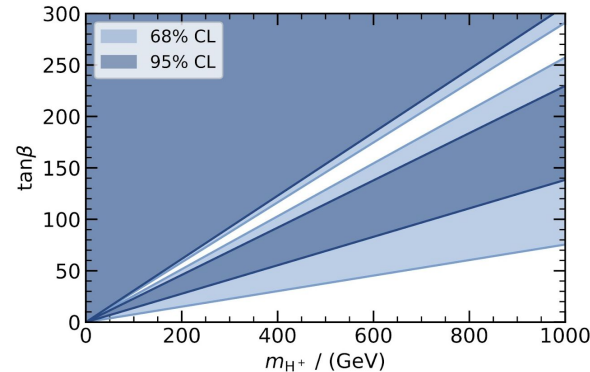
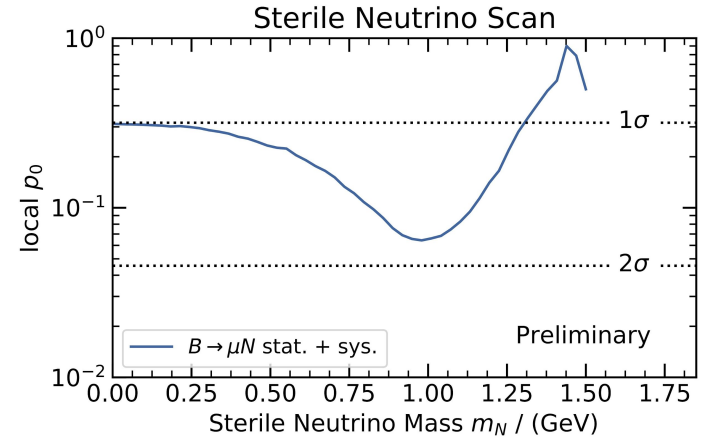
- 2018 result (*top*):
  - Untagged
  - Hunt for bump in  $p_\mu$
  - World's best BF ( $2.4\sigma$  significance)
- 2019 extension (**preliminary**; Moriond EW, *bottom*):
  - Inclusive tagging
  - Systematics improvements
  - Investigate type-II and -III 2HDM
  - Sterile neutrino scan



# Belle: update to $B^- \rightarrow \mu^- \nu$

## Preliminary update to Belle 2018 PRL

- Preliminary results:
  - Improved significance:  $2.8\sigma$
  - Sterile neutrino scan
  - 2HDM limits





# Prospects

What can we expect in the future?

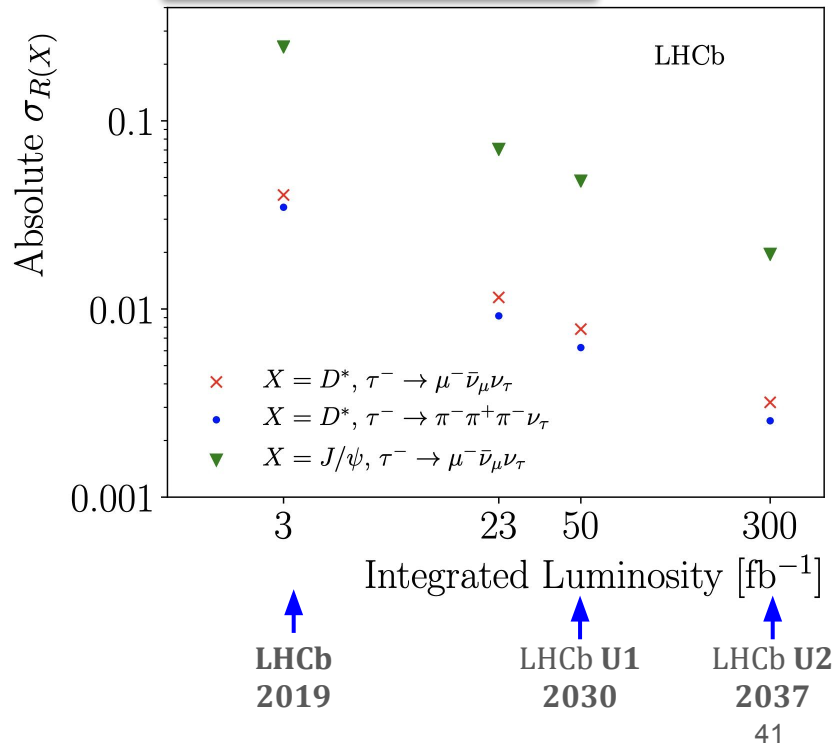
Belle II physics book, 2018  
[arxiv:1808.10567](https://arxiv.org/abs/1808.10567)

Process	Observable	Theory	Sys. dom. (Discovery) [ab <sup>-1</sup> ]	vs LHCb	vs Belle	Anomaly	NP
● $B \rightarrow \pi \ell \nu_\ell$	$ V_{ub} $	***	10-20	***	***	**	*
● $B \rightarrow X_u \ell \nu_\ell$	$ V_{ub} $	**	2-10	***	**	***	*
● $B \rightarrow \tau \nu$	$Br.$	***	>50 (2)	***	***	*	***
● $B \rightarrow \mu \nu$	$Br.$	***	>50 (5)	***	***	*	***
● $B \rightarrow D^{(*)} \ell \nu_\ell$	$ V_{cb} $	***	1-10	***	**	**	*
● $B \rightarrow X_c \ell \nu_\ell$	$ V_{cb} $	***	1-5	***	**	**	**
● $B \rightarrow D^{(*)} \tau \nu_\tau$	$R(D^{(*)})$	***	5-10	**	***	***	***
● $B \rightarrow D^{(*)} \tau \nu_\tau$	$P_\tau$	***	15-20	***	***	**	***
● $B \rightarrow D^{**} \ell \nu_\ell$	$Br.$	*	-	**	***	**	-



↑  
**50ab<sup>-1</sup>**  
**2027**

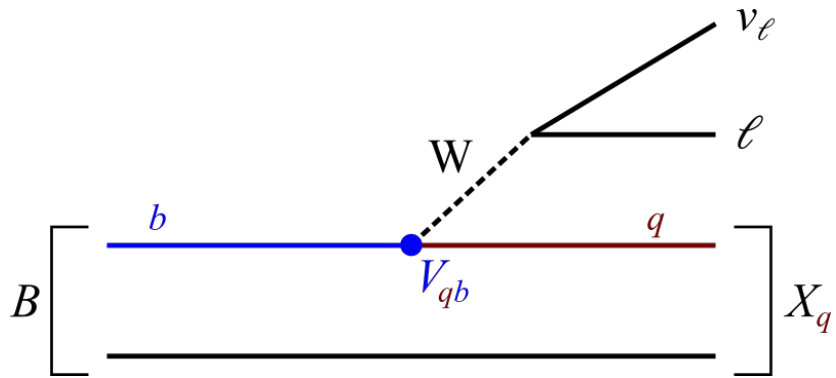
Physics case for an LHCb Upgrade II, 2018  
[arxiv:1808.08865](https://arxiv.org/abs/1808.08865)



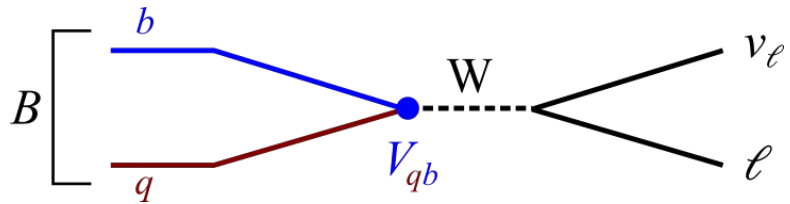
# Summary

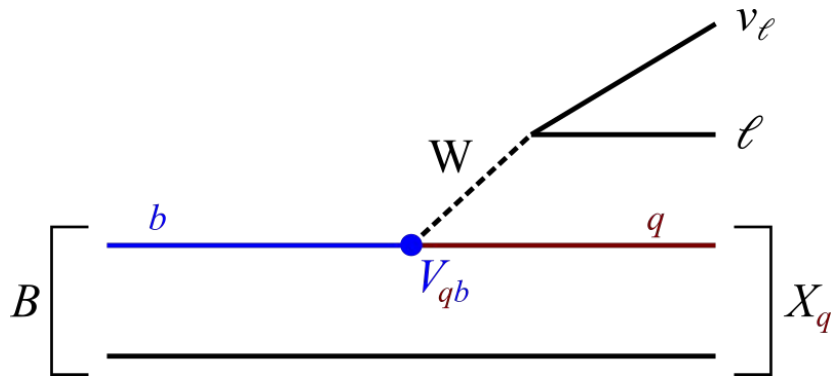
## Mysteries still mysterious

- Inclusive/exclusive tension in  $V_{ub}/V_{cb}$ 
  - Form factor dependence (probably) won't save us
  - Tension still at  $\sim 3\sigma$
- Excess in  $R(D^{(*)})$ 
  - World average tension with SM still at  $\sim 3\sigma$ , but decreasing
- Semileptonic and leptonic B decays remain **excellent probes** of SM and BSM physics
- **Eagerly awaiting Belle II and upgraded LHCb results!**

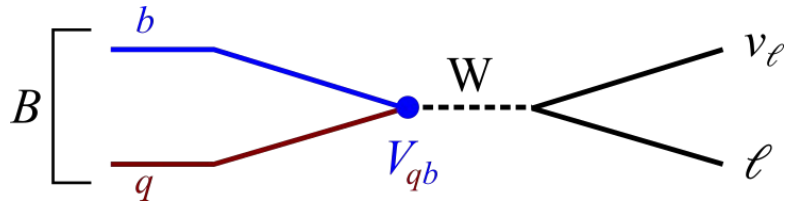


THANK YOU!





ADDITIONAL SLIDES



# The $B$ factories

## Kinematics

- We know the beam energy ( $m_{Y(4S)}$ )
- Define two  $\sim$ -independent kinematic quantities
  - $\Delta E = E_B^* - E_{\text{beam}}^*$  ( $\sim 0$  for true  $B$ )
  - $m_{bc} = \sqrt{E_{\text{beam}}^{*2} - \mathbf{p}_B^{*2}}$  ( $\sim m_B$  for true  $B$ )
  - *Kinematic consistency* of reconstructed  $B$  with  $B$  meson
- For single-neutrino decays, define  $Y$  as the visible mass in the decay. Then this quantity should be in  $[-1, 1]$ 
  - $$\cos \theta_{BY} = \frac{2E_B E_Y - m_B^2 - m_Y^2}{2p_B p_Y}$$

