

Semileptonic and rare heavy flavour decays at LHCb

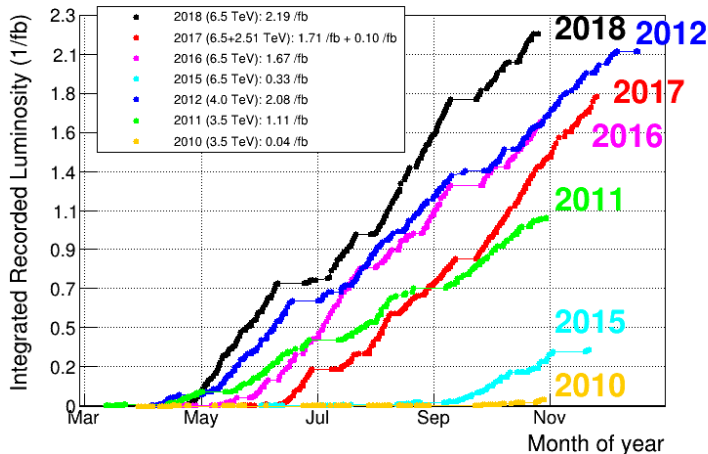
PIC 2019, Taipei

Mark Smith on behalf of the LHCb collaboration

September 2019



Imperial College
London



Data collected:

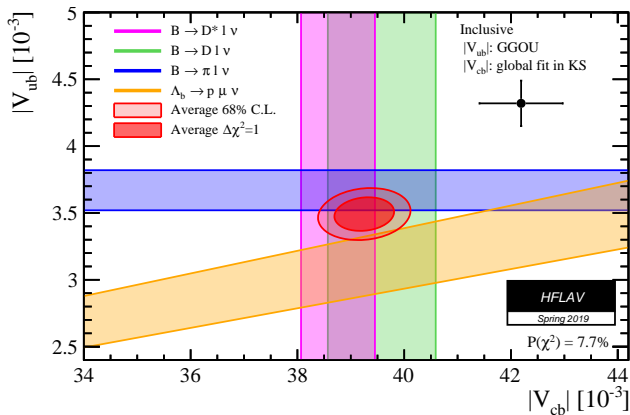
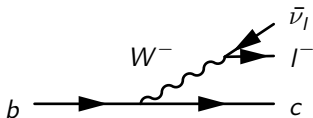
- Run 1 : 3 fb^{-1} at 7–8 TeV
- Run 2 : 6 fb^{-1} at 13 TeV

$\sigma(pp \rightarrow B^\pm X)$: JHEP 12, 026 (2017)

- 7 TeV - $43.0 \pm 0.2 \pm 2.5 \pm 1.7 \mu\text{b}$.
- 13 TeV - $86.6 \pm 0.5 \pm 5.4 \pm 3.4 \mu\text{b}$.

Semileptonic decays

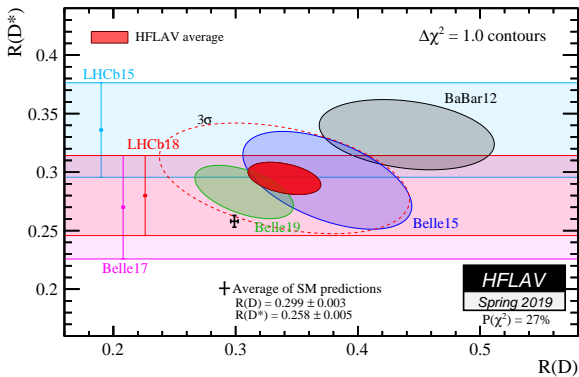
- Copious
- Theoretically 'clean' - FFs
- Access to CKM elements
- Experimentally difficult - neutrinos



LHCb:
 Nature Physics 11,
 743 (2015)

Semileptonic decays

$$R(D^{(*)}) = \frac{\mathcal{B}(B \rightarrow D^{(*)} \tau \nu_\tau)}{\mathcal{B}(B \rightarrow D^{(*)} \mu \nu_\mu)}$$



BaBar:

PRL 109, 101802 (2012)

PRD 88, 072012 (2013)

Belle:

PRD 92, 072014 (2015)

PRL 118, 211801 (2017)

PRD 97, 012004 (2018)

arXiv:1904.08794 (2019)

LHCb:

PRL 120, 171802 (2018)

PRD 97, 072013 (2018)

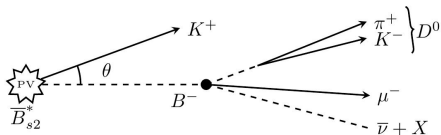
PRL 115, 111803 (2015)

Uncertainty from $B \rightarrow D^{**} l^+ \nu_l$

$B \rightarrow D^0 \mu^- \nu_\mu X$ branching fractions

Run 1 dataset - 3 fb^{-1} at 7–8 TeV:

Take B^- from $\bar{B}_{s2}^* \rightarrow B^- K^+$ and constrain B^- kinematics.

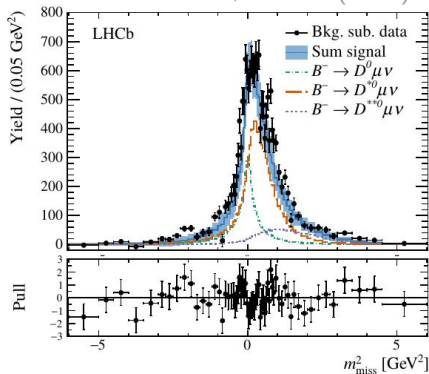


Fit m_{miss}^2 for $B^- \rightarrow D^0 \mu^- \bar{\nu}_\mu X$ components.

BFs of $B^- \rightarrow D^0 \mu^- \bar{\nu}_\mu$, $B^- \rightarrow D^{*0} \mu^- \nu_\mu$, $B^- \rightarrow D^{**0} \mu^- \nu_\mu$:

$$f_{D^0} = \frac{\mathcal{B}(B^- \rightarrow D^0 \mu^- \bar{\nu}_\mu)}{\mathcal{B}(B^- \rightarrow D^0 \mu^- \bar{\nu}_\mu X)}$$

PRD 99, 092009 (2019)



$$f_{D^0} = 0.25 \pm 0.06$$

$$f_{D^{**0}} = 0.21 \pm 0.07$$

$$f_{D^{*0}} = 1 - f_{D^0} - f_{D^{**0}}$$

All hadron species at LHCb!

Consider B_c decays in Run 1:

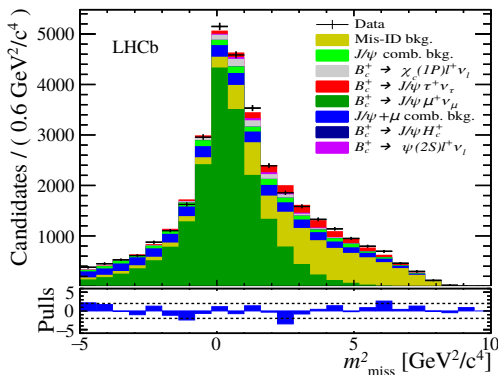
- Take $\tau^+ \rightarrow \mu^+ \bar{\nu}_\tau \nu_\mu$ (17.4%)
- 3D template fit to kinematic variables

$$R(J/\psi) = \frac{\mathcal{B}(B_c^+ \rightarrow J/\psi \tau^+ \nu_\tau)}{\mathcal{B}(B_c^+ \rightarrow J/\psi \mu^+ \nu_\mu)}$$

$$= 0.71 \pm 0.17 \pm 0.18$$

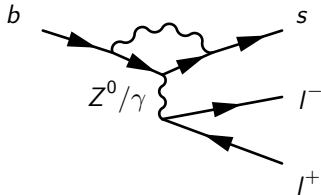
Major systematics:

- Simulation stats: **Reducible**
- $B_c \rightarrow J/\psi$ FF: **Reducible with lattice** - see [here](#)



Compatible with SM expectations at $\sim 2\sigma$

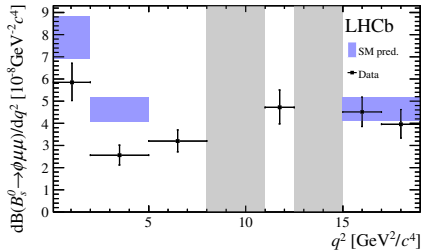
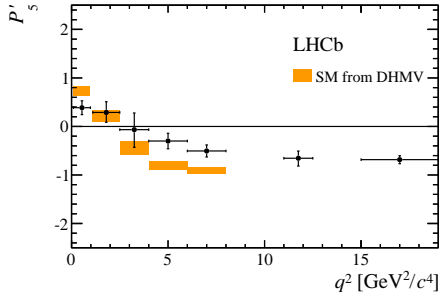
Rare decays



FCNC are rare processes
 Good place to look for NP!

Some deviations from the SM observed
 in $b \rightarrow s l^- l^+$:

- $B \rightarrow K^* \mu^+ \mu^-$ angular analysis
 JHEP 1602, 104 (2016)
- $d\mathcal{B}(B_s^0 \rightarrow \phi \mu^+ \mu^-)/dq^2$
 JHEP 09, 179 (2015)
- $d\mathcal{B}(B^+ \rightarrow K^+ \mu^+ \mu^-)/dq^2$
 JHEP 06, 133 (2014)



A question of hadronic uncertainties?

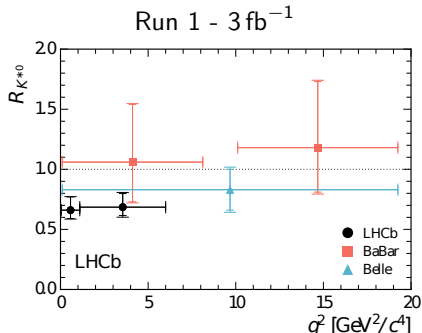
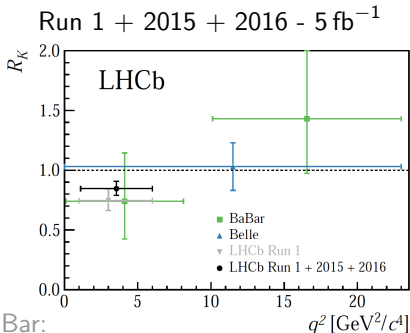
$$R_{K^{(*)}}$$

Test of lepton universality - theoretically clean.

PRL 122, 191801 (2019)

JHEP 08, 055 (2017)

$$R(K^{(*)}) = \frac{\int_{q_{min}^2}^{q_{max}^2} \frac{d\Gamma[B \rightarrow K^{(*)} \mu^+ \mu^-]}{dq^2} dq^2}{\int_{q_{min}^2}^{q_{max}^2} \frac{d\Gamma[B \rightarrow K^{(*)} e^+ e^-]}{dq^2} dq^2}$$



BaBar:

PRD 86, 032012 (2012)

Belle:

PRL 103, 171801 (2009)

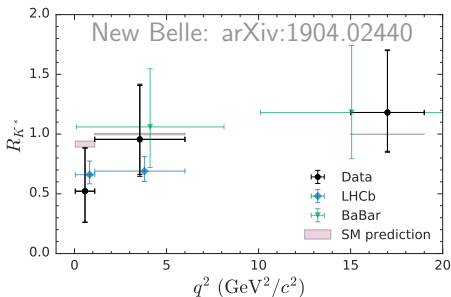
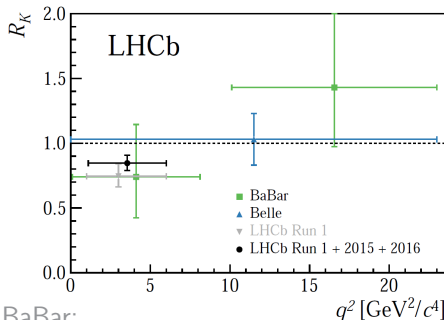
Best precision from LHCb
Deviations from SM of $\sim 2.5 \sigma$

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BaBar:

PRD 86, 032012 (2012)

Belle:

PRL 103, 171801 (2009)

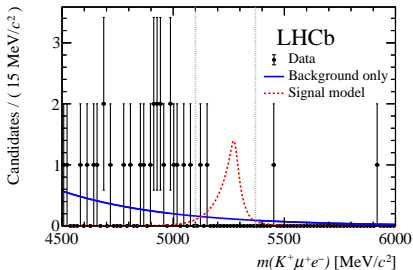
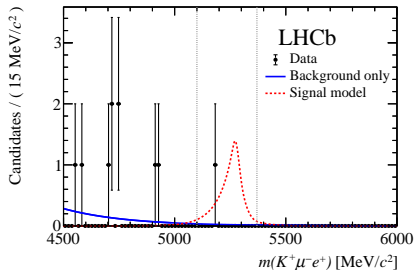
Best precision from LHCb
 Deviations from SM of $\sim 2.5 \sigma$

$$B^+ \rightarrow K^+ \mu^\pm e^\mp$$

Run 1 dataset - 3 fb^{-1} at 7–8 TeV:

arXiv:1909.01010

- Lepton flavour violation forbidden in SM.
- Models to explain $b \rightarrow sll$ can lead to LFV.
- BF of order 10^{-8} possible. JHEP 06, 072 (2015)



Mode	Expected	Observed	90% CL limit
$B^+ \rightarrow K^+ \mu^+ e^-$	3.9 ± 1.1	2	6.4×10^{-9}
$B^+ \rightarrow K^+ \mu^- e^+$	0.9 ± 0.6	1	7.0×10^{-9}

Order of magnitude improvement on previous BaBar limits

PRD 73, 092001 (2006)

$$B_{(s)}^0 \rightarrow \tau^\pm \mu^\mp$$

Run 1 dataset - 3 fb^{-1} at 7–8 TeV

Search for B^0 and B_s^0 decays:

- Hadronic τ^+ decay:

$$\tau^+ \rightarrow \pi^+ \pi^- \pi^+ \bar{\nu}_\tau$$

- Can solve the B kinematics with a twofold ambiguity.
- Peak in M_B

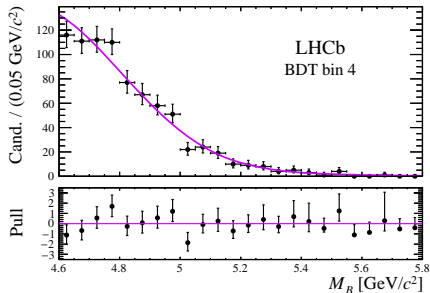
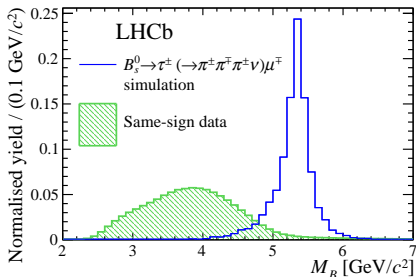
No signal, limits set at 90% CL:

$$\mathcal{B}(B_s^0 \rightarrow \tau^\pm \mu^\mp) < 3.4 \times 10^{-5}$$

$$\mathcal{B}(B^0 \rightarrow \tau^\pm \mu^\mp) < 1.2 \times 10^{-5}$$

- Factor 2 improvement for B^0 wrt BaBar search
PRD 77, 091104 (2008)
- First search for B_s^0

arXiv:1905.06614



$$B^+ \rightarrow \mu^+ \mu^- \mu^+ \nu_\mu$$

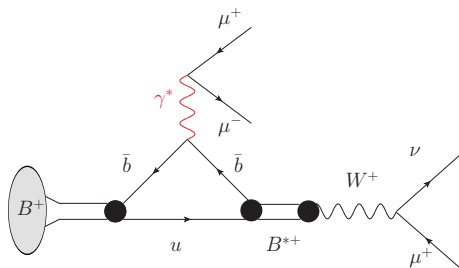
Run 1 + 2016 datasets

- $B^+ \rightarrow \mu^+ \nu_\mu$ helicity suppressed.
- Belle: $(6.46 \pm 2.22 \pm 1.60) \times 10^{-7}$
PRL 121, 031801 (2018)
- Scope for observable new physics.
- One track final state.

Include $\gamma^* \rightarrow \mu^+ \mu^-$:

- Lift helicity suppression
- 3-track vertex

EPJC 79, 675 (2019)



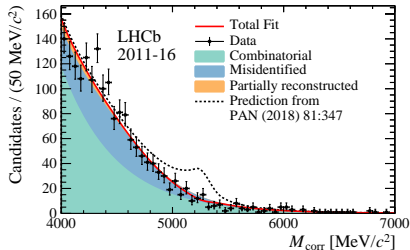
Fit corrected mass

$$m_{corr} = \sqrt{M_{\mu\mu\mu}^2 + |p_\perp^2| + |p_\perp|}$$

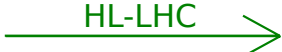
peaks at B mass when missing a ν_μ .

No signal seen - limit set:

$$\mathcal{B}(B^+ \rightarrow \mu^+ \mu^- \mu^+ \nu_\mu) < 1.6 \times 10^{-8}$$



Looking forward at LHCb

			HL-LHC 	
7 - 8 TeV	13 TeV	14 TeV		
Run 1 2010 - 2012	Run 2 2015 - 2018	Run 3 2021 - 2023	Run 4 2026 - 2029	Run 5 2031 -
3 fb^{-1}	9 fb^{-1}	23 fb^{-1}	50 fb^{-1}	300 fb^{-1}

↑ Upgrade I ↑ Upgrade II

Upgrade I:

[CERN-LHCC-2012-007](#)

Upgrade II:

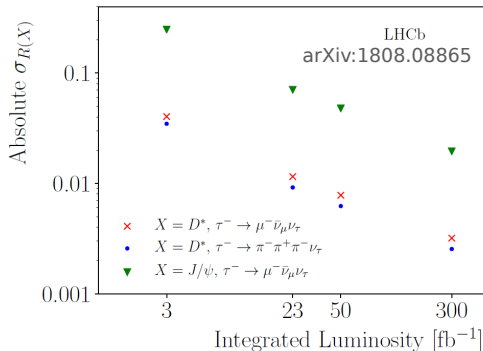
[CERN-LHCC-2017-003](#)

Much work done:

- LHCb has much high quality data.

Much work to be done:

- Many (unique) measurements still to make.
- **These are exciting times.**



BACKUP

Semi-leptonic B decays at the LHC



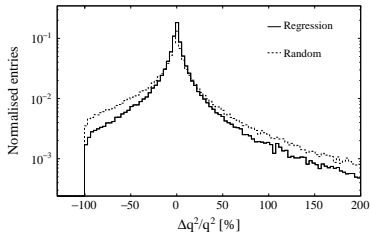
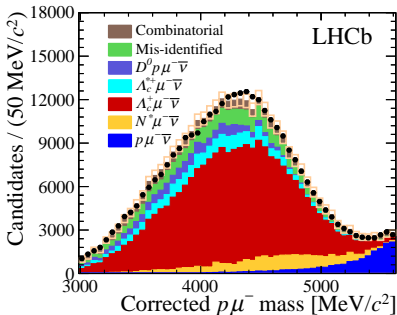
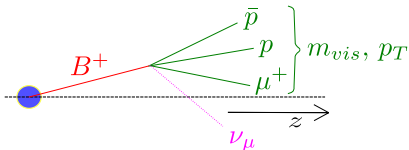
- High branching fraction: $\mathcal{BF}(B \rightarrow Xl\nu_l) \approx 10\%$.
- Theoretically 'clean' \rightarrow only calculate one hadronic current.
- Large B production cross-section.
- Large quantity of Λ_b , B_s and B_c .
- Muon to trigger on at L0.



- Partially reconstructed signal.
- No beam energy constraint.
- Hard to make an exclusive HLT selection. Use an MVA.
- Many backgrounds.
- Need lots of simulation.

Semi-leptonic B decays at the LHC

Ascertain B kinematics up to two-fold ambiguity. Ciezarek et al. JHEP (2017):21

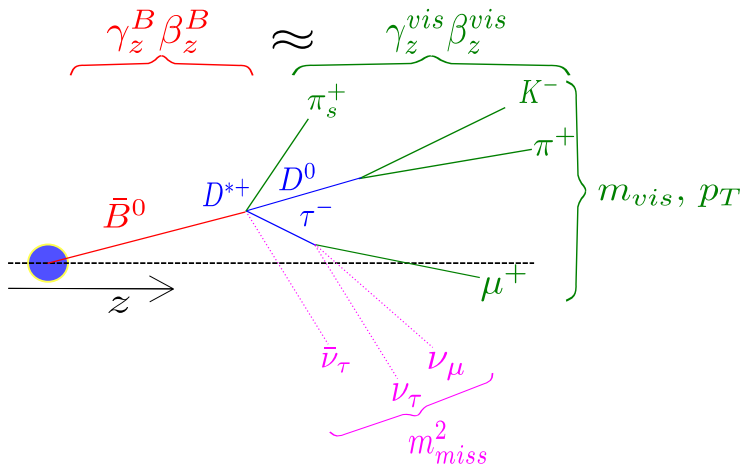


Estimate *corrected* mass:

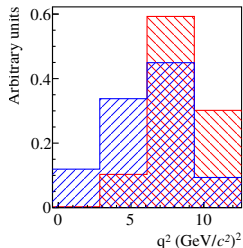
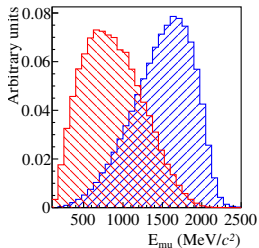
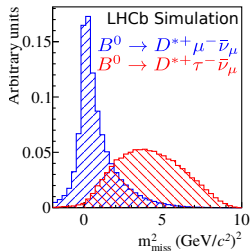
$$m_{corr} = |p'_T| + \sqrt{|p'_T|^2 + m_{vis}^2}$$

p'_T is visible momentum transverse to B flight.

τ reconstruction : $\tau^+ \rightarrow \mu^+ \bar{\nu}_\tau \nu_\mu$ (17.4%)



Variable	Definition	μ	τ
m_{miss}^2	$(p_B - p_{vis})^2$	peaks at 0	> 0
q^2	$(p_B - p_{D^*})^2$	$0 \text{ MeV} < q^2 < 3270 \text{ MeV}$	$m_\tau < q^2 < 3270 \text{ MeV}$
E_μ^*	E_μ in B frame	hard	soft

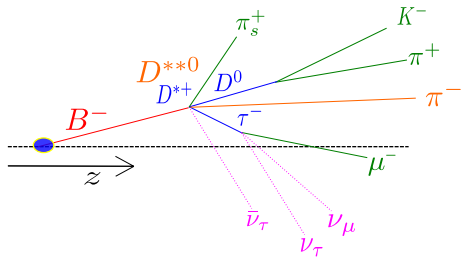


- 3D template fit.

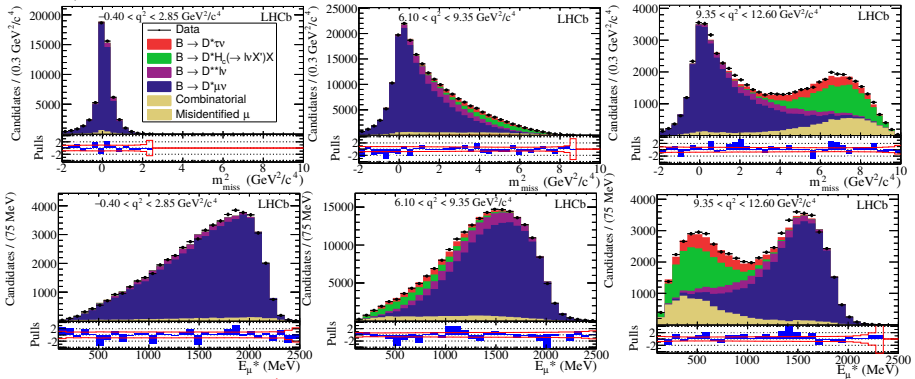
- μ mis-ID and combinatorial taken from data.
- All other templates from simulation with systematic variations.

- Major backgrounds:

- $B \rightarrow D^{**} \mu \nu$
- $B \rightarrow D^{*+} X_c, X_c \rightarrow X \mu \nu$
- Reduce with charged isolation.



Run 1, 3fb^{-1} :



$$R(D^*) = 0.336 \pm 0.027(\text{stat}) \pm 0.030(\text{syst})$$

2.1 σ deviation from SM prediction

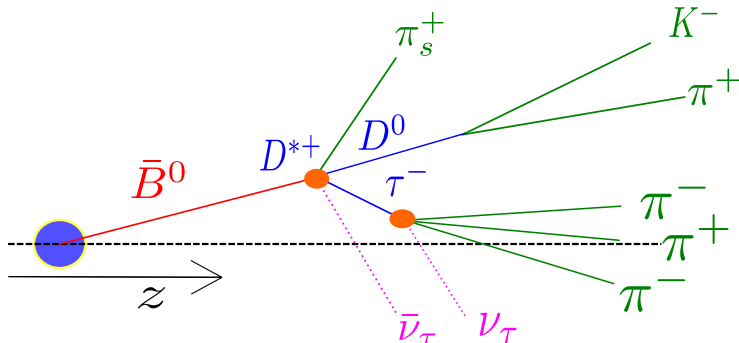
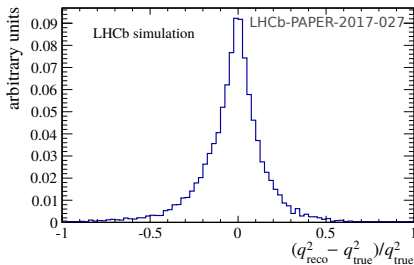
Major systematics:

- Simulation sample size \rightarrow reducible
- mis-ID sample size \rightarrow reducible
- $B \rightarrow D^* \tau \nu$ form-factor \rightarrow scale with data

τ reconstruction : $\tau^+ \rightarrow \pi^+ \pi^- \pi^+ \bar{\nu}_\tau (\pi^0)$ (13.9%)

$$K(D^*) = \frac{\mathcal{B}(B \rightarrow D^* \tau \nu_\tau)}{\mathcal{B}(B \rightarrow D^* \pi^+ \pi^- \pi^+)}$$

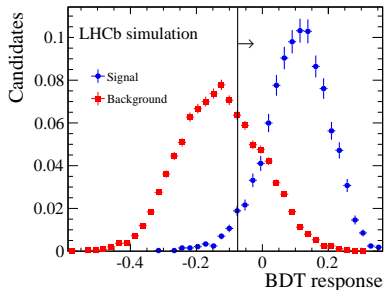
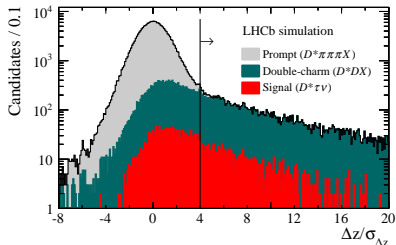
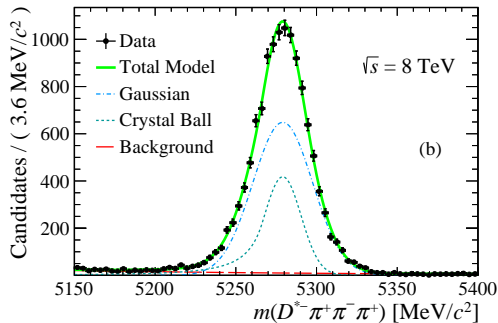
- Require external input to turn $K(D^*)$ into $R(D^*)$.
- Reconstructable τ decay vertex \rightarrow background reduction!
- Estimate B kinematics (backup).

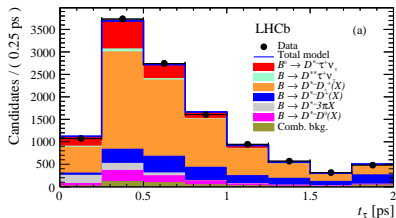
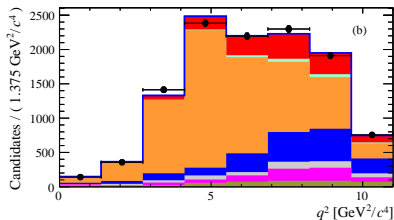


Major backgrounds:

- $B \rightarrow D^{*+} \pi^+ \pi^- \pi^- X$.
 - Reduced with τ flight distance cut.
- $B \rightarrow D^{*+} X_C$
 - $X_C \rightarrow \pi^+ \pi^- \pi^- X$.
 - Reduced with a multivariate discriminator.

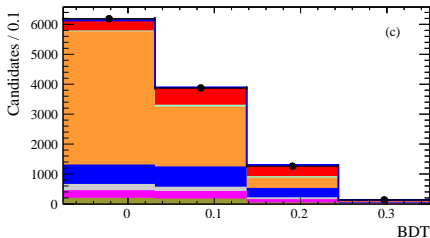
Normalisation fit to $m(D^{*+} 3\pi)$:



Run 1, 3fb^{-1} . Fit q^2 , t_τ , BDT classifier:

Systematics:

- Simulation sample size
- Double charm background
- $D^{*-} 3\pi X$ background
- $D^{**} \tau \nu_\tau$ feed-down



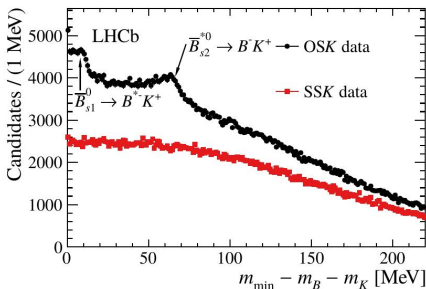
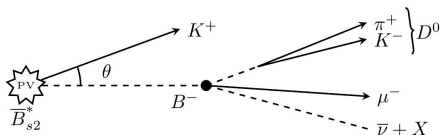
$$R(D^{*-}) = 0.291 \pm 0.019(\text{stat}) \pm 0.026(\text{syst}) \pm 0.013(\text{BR})$$

$B \rightarrow D^0 \mu^- \nu_\mu X$ branching fractions

$B \rightarrow D \mu^+ \nu_\mu X$ background significant source of uncertainty - **measure it!**

LHCb-PAPER-2018-024

Take B^- from $\bar{B}_{s2}^* \rightarrow B^- K^+$ and constrain B^- kinematics.



- Quadratic equation for $B^- K^+$ energy \rightarrow pick minimum value for real solution.

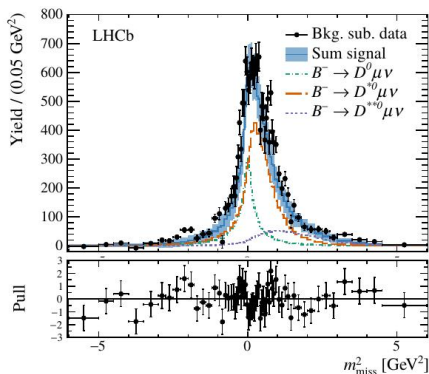
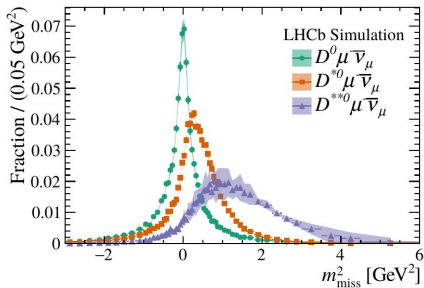
$$m_{\min} = \sqrt{m_B^2 + m_K^2 + 2m_B \sqrt{p_K^2 \sin^2 \theta + m_K^2}}$$

- Constrain signal and background from $m_{\min} - m_B - m_K$ distribution.
- Calculate m_{miss}^2 assuming the signal decay.

$B \rightarrow D^0 \mu^- \bar{\nu}_\mu X$ branching fractions

Fit m_{miss}^2 for $B^- \rightarrow D^0 \mu^- \bar{\nu}_\mu X$ components.

LHCb-PAPER-2018-024



Relative BFs of $B^- \rightarrow D^0 \mu^- \bar{\nu}_\mu$, $B^- \rightarrow D^{*0} \mu^- \bar{\nu}_\mu$, $B^- \rightarrow D^{**0} \mu^- \bar{\nu}_\mu$:

$$f_{D^0} = 0.25 \pm 0.06$$

$$f_{D^{**0}} = 0.21 \pm 0.07$$

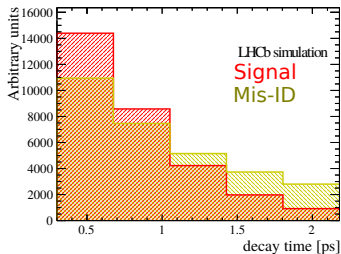
$$f_{D^{*0}} = 1 - f_{D^0} - f_{D^{**0}}$$

$$R(J/\psi) = \frac{\mathcal{B}(B_c^+ \rightarrow J/\psi \tau^+ \nu_\tau)}{\mathcal{B}(B_c^+ \rightarrow J/\psi \mu^+ \nu_\mu)} \quad \tau^+ \rightarrow \mu^+ \bar{\nu}_\tau \nu_\mu$$

- Probing same physics as $R(D^*)$. SM expectation 0.25–0.28.
Phys. Lett. B452 (1999) 129, arXiv:hep-ph/0211021,
Phys. Rev. D73 (2006) 054024, Phys. Rev. D74 (2006) 074008
- Only available at LHCb.

As per $R(D^*)$ use kinematic distributions:
 $m_{miss}^2, Z(q^2, E_\mu^2)$.

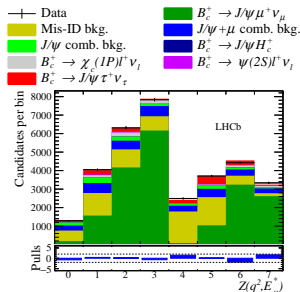
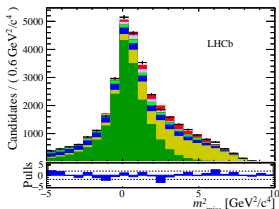
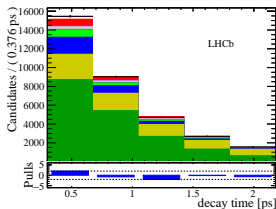
- Additionally consider B_c^+ decay-time.
- $B_c^+ \rightarrow J/\psi$ form-factors are unknown - estimated from fit to enriched sample of the normalisation mode.



3D template fit: B_c decay-time, m_{miss}^2 , Z .

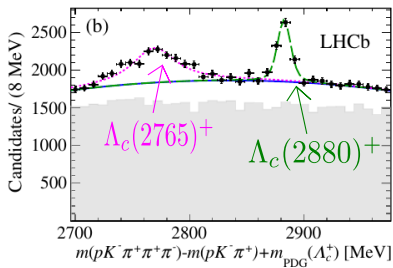
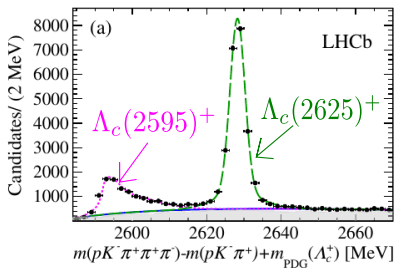
$$R(J/\psi) = 0.71 \pm 0.17 \pm 0.18$$

- Compatible with SM at 2σ .
- First evidence of decay $B_c^+ \rightarrow J/\psi \tau^+ \nu_\tau$
- Largest systematics from $B_c \rightarrow J/\psi$ form-factor and limited simulation sample size - **both can be improved.**
- Lattice form-factor calculation is on the way - see [here](#)



We can measure $\Lambda_b \rightarrow \Lambda_c^+ \mu^- \nu_\mu$ differential BF \rightarrow form-factor shape.

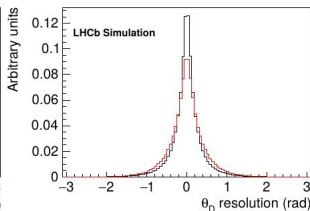
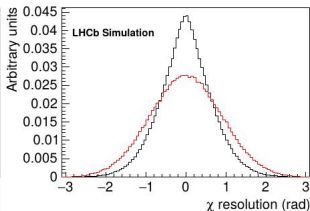
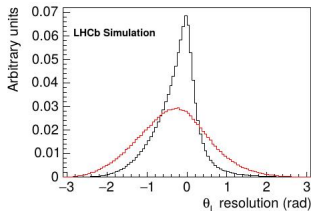
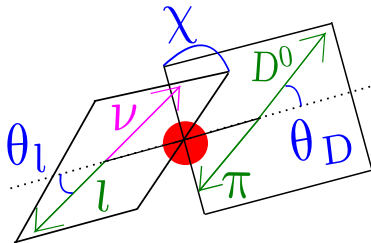
- Measure yield of $\Lambda_b \rightarrow \Lambda_c^+ \mu^- \nu_\mu$ in 14 bins of $1 < w < 1.43$.
- Take lower q^2 solution.
- Correct for selection efficiency.
- Correct for feed-down from $\Lambda_c^{*+} \rightarrow \Lambda_c^+ \pi^+ \pi^-$ - extracted from data.
- Unfold w resolution.



Angular analyses?

If the tension persists we can learn more about new physics with angular and kinematic variables.

- BaBar has compared q^2 with theory: [PRD 88, 072012 \(2013\)](#)
- Belle has measured τ polarisation: [PRL 118, 211801 \(2017\)](#)
- Unfolding needs careful consideration at LHCb.

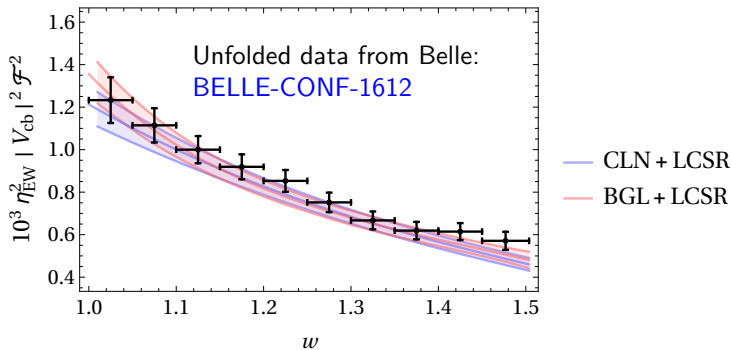


Approximate $\gamma_z^B \beta_z^B \approx \gamma_z^{\text{vis}} \beta_z^{\text{vis}}$ - $B \rightarrow D^* \mu \nu$, $B \rightarrow D^* \tau \nu$, $\tau \rightarrow \mu \nu \nu$

Theoretical uncertainties

Bigi, Gambino, Schacht: [PLB 769, 441-445 \(2017\)](#)

Grinstein, Kobach: [PLB 771, 359-364 \(2017\)](#)



	BGL: Data + lattice	CLN: Data + lattice
$ V_{cb} $	$0.0417^{(+20}_{-21)}$	$0.0382(15)$

- Slight change in $R(D) - R(D^*)$ prediction.
- Hard to make a model independent measurement.

More data needed → [new Belle result!](#)

Hadronic $R(D^*)$ - kinematics

Two-fold ambiguity in determining τ momentum:

$$|\mathbf{p}_\tau| = \frac{(m_{3\pi}^2 + m_\tau^2) |\mathbf{p}_{3\pi}| \cos \theta_{\tau,3\pi} \pm E_{3\pi} \sqrt{(m_\tau^2 - m_{3\pi}^2)^2 - 4m_\tau^2 |\mathbf{p}_{3\pi}|^2 \sin^2 \theta_{\tau,3\pi}}}{2(E_{3\pi}^2 - |\mathbf{p}_{3\pi}|^2 \cos^2 \theta_{\tau,3\pi})}$$

where $\theta_{\tau,3\pi}$ is the angle between the 3π system 3-momentum and the τ flight.
Take maximum allowed angle:

$$\theta_{\tau,3\pi}^{\max} = \arcsin \left(\frac{m_\tau^2 - m_{3\pi}^2}{2m_\tau |\mathbf{p}_{3\pi}|} \right)$$

Same for B momentum where Y represents the $D^{*-} \tau^+$ system:

$$|\mathbf{p}_{B^0}| = \frac{(m_Y^2 + m_{B^0}^2) |\mathbf{p}_Y| \cos \theta_{B^0,Y} \pm E_Y \sqrt{(m_{B^0}^2 - m_Y^2)^2 - 4m_{B^0}^2 |\mathbf{p}_Y|^2 \sin^2 \theta_{B^0,Y}}}{2(E_Y^2 - |\mathbf{p}_Y|^2 \cos^2 \theta_{B^0,Y})}$$

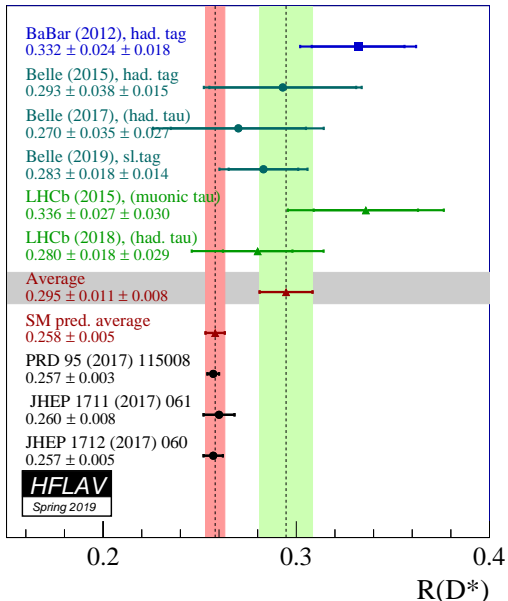
with:

$$\theta_{B^0,Y}^{\max} = \arcsin \left(\frac{m_{B^0}^2 - m_Y^2}{2m_{B^0} |\mathbf{p}_Y|} \right)$$

Table 1: Systematic uncertainties in the extraction of $\mathcal{R}(D^*)$.

Model uncertainties	Absolute size ($\times 10^{-2}$)
Simulated sample size	2.0
Misidentified μ template shape	1.6
$\bar{B}^0 \rightarrow D^{*+}(\tau^-/\mu^-)\bar{\nu}$ form factors	0.6
$\bar{B} \rightarrow D^{*+}H_c(\rightarrow \mu\nu X')X$ shape corrections	0.5
$\mathcal{B}(\bar{B} \rightarrow D^{**}\tau^-\bar{\nu}_\tau)/\mathcal{B}(\bar{B} \rightarrow D^{**}\mu^-\bar{\nu}_\mu)$	0.5
$\bar{B} \rightarrow D^{**}(\rightarrow D^*\pi\pi)\mu\nu$ shape corrections	0.4
Corrections to simulation	0.4
Combinatorial background shape	0.3
$\bar{B} \rightarrow D^{**}(\rightarrow D^{*+}\pi)\mu^-\bar{\nu}_\mu$ form factors	0.3
$\bar{B} \rightarrow D^{*+}(D_s \rightarrow \tau\nu)X$ fraction	0.1
Total model uncertainty	2.8

$R(D^*)$ average



$\Lambda_b \rightarrow \Lambda_c^+ \mu^- \nu_\mu$ decay described by 6 FF.

- Take infinite heavy quark mass \rightarrow Isgur-Wise function $\xi_B(w)$

$$w = v_{\Lambda_b} \cdot v_{\Lambda_c^+} = (m_{\Lambda_b}^2 + m_{\Lambda_c^+}^2 - q^2)/2m_{\Lambda_b}m_{\Lambda_c^+}$$

- Differential decay rate:

$$\frac{d\Gamma}{dw} = GK(w)\xi_B^2(w)$$

G is a constant, $K(w)$ is a known kinematic factor.

Parametrise $\xi_B(w)$, i.e. with Taylor expansion:

$$\xi_B(w) = 1 - \rho^2(w - 1) + \frac{1}{2}\sigma^2(w - 1)^2 + \dots$$

ρ^2	Approach	Ref.
1.35 ± 0.13	QCD sum rules	PLB 629, 27 (2005)
$1.2_{-1.1}^{+0.8}$	Lattice	PRD 57, 6948 (1998)
1.51	HQET + relativistic wave function	PRD 73, 094002 (2006)